



## Antenas Abertura



Pyramidal horn antenna



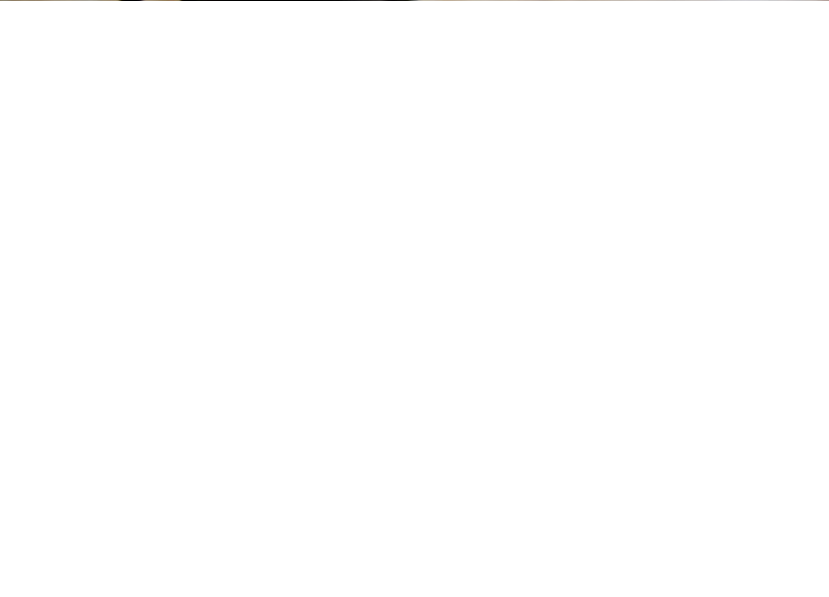
Conical horn antenna

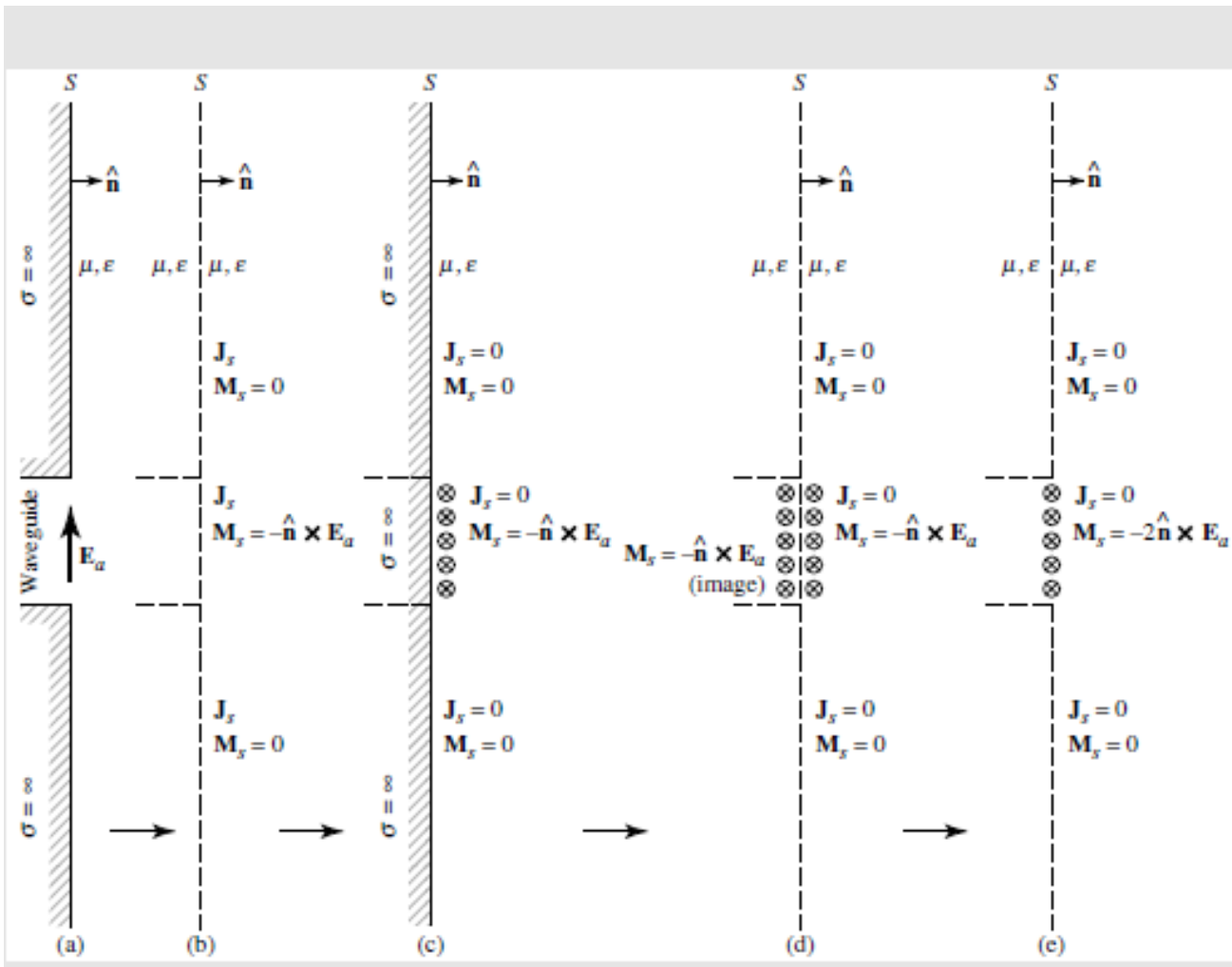


Paraboloidal antenna



Slot antenna





$$E_r \simeq 0 \quad (12-10a)$$

$$E_\theta \simeq -\frac{jke^{-jkr}}{4\pi r}(L_\phi + \eta N_\theta) \quad (12-10b)$$

$$E_\phi \simeq +\frac{jke^{-jkr}}{4\pi r}(L_\theta - \eta N_\phi) \quad (12-10c)$$

$$H_r \simeq 0 \quad (12-10d)$$

$$H_\theta \simeq \frac{jke^{-jkr}}{4\pi r} \left( N_\theta - \frac{L_\theta}{\eta} \right) \quad (12-10e)$$

$$H_\phi \simeq -\frac{jke^{-jkr}}{4\pi r} \left( N_\phi + \frac{L_\phi}{\eta} \right) \quad (12-10f)$$

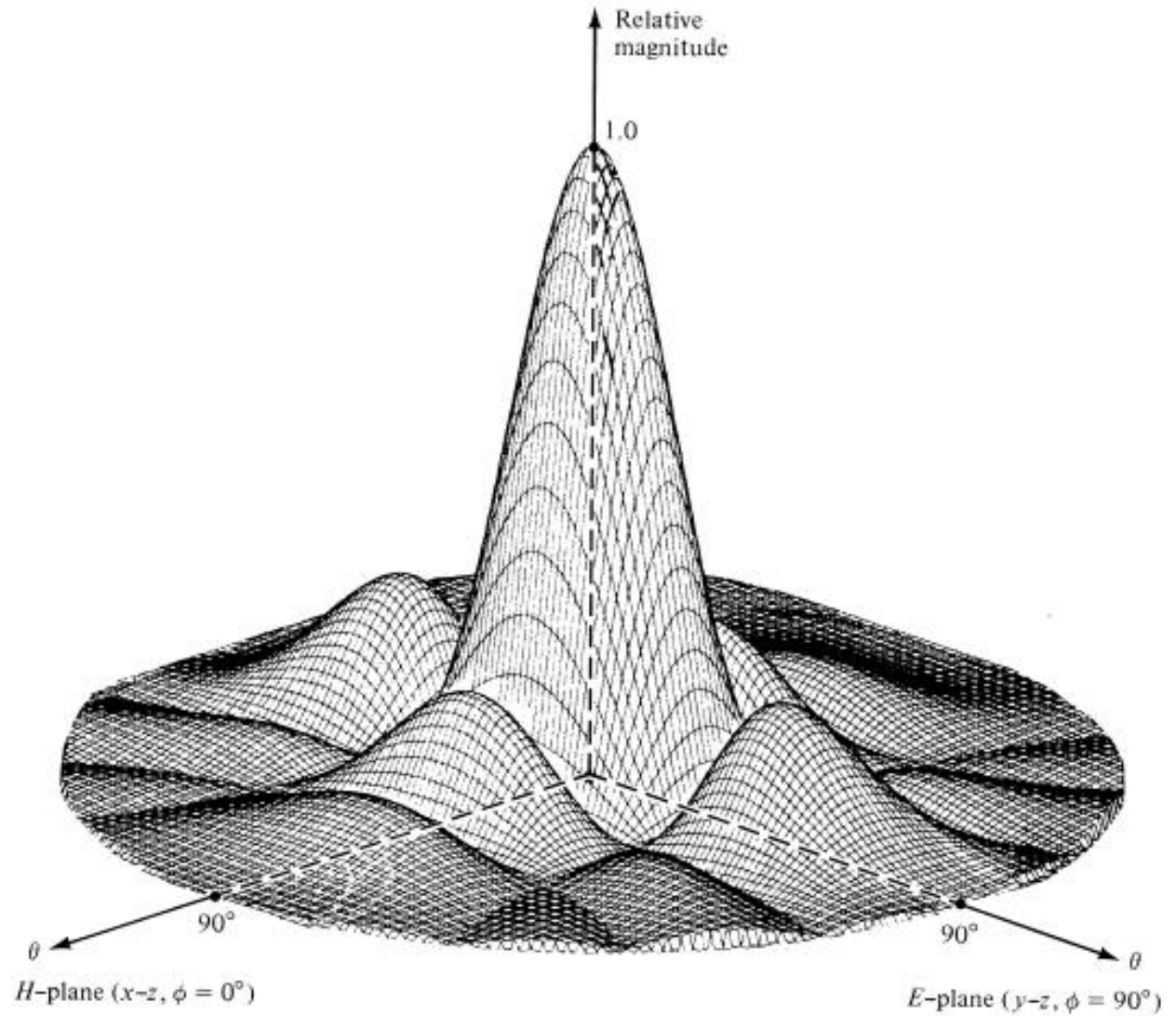
$$N_\theta = \iint_S [J_x \cos \theta \cos \phi + J_y \cos \theta \sin \phi - J_z \sin \theta] e^{+jkr' \cos \psi} ds' \quad (12-12a)$$

$$N_\phi = \iint_S [-J_x \sin \phi + J_y \cos \phi] e^{+jkr' \cos \psi} ds' \quad (12-12b)$$

$$L_\theta = \iint_S [M_x \cos \theta \cos \phi + M_y \cos \theta \sin \phi - M_z \sin \theta] e^{+jkr' \cos \psi} ds' \quad (12-12c)$$

$$L_\phi = \iint_S [-M_x \sin \phi + M_y \cos \phi] e^{+jkr' \cos \psi} ds' \quad (12-12d)$$

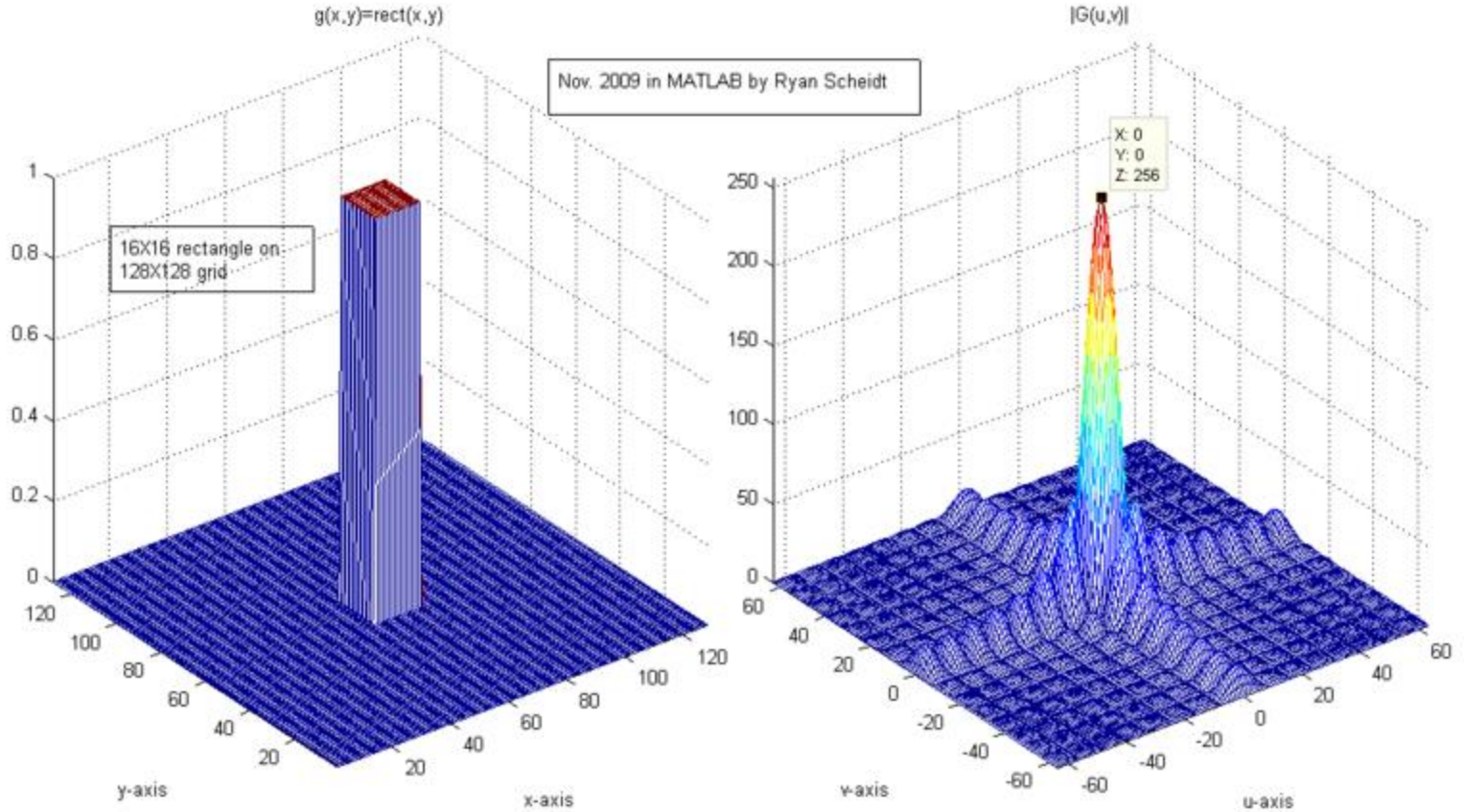
Conheço J ou M !



**Figure 12.8** Three-dimensional field pattern of a constant field rectangular aperture mounted on an infinite ground plane ( $a = 3\lambda$ ,  $b = 2\lambda$ ).



# 2D Fourier Transform – rect $\rightarrow$ sinc

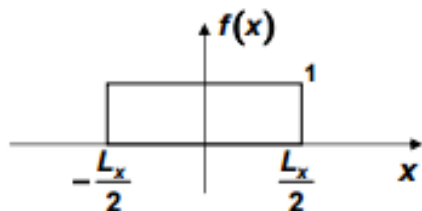


## Fourier Transforms and the Rectangular Aperture Far-Field

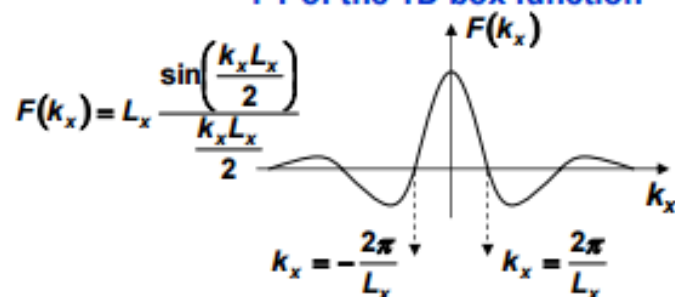
FT:  $F(k_x) = \int_{-\infty}^{\infty} f(x) e^{jk_x x} dx$

IFT:  $f(x) = \int_{-\infty}^{\infty} F(k_x) e^{-jk_x x} \frac{dk_x}{2\pi}$

Consider the 1D box function



FT of the 1D box function



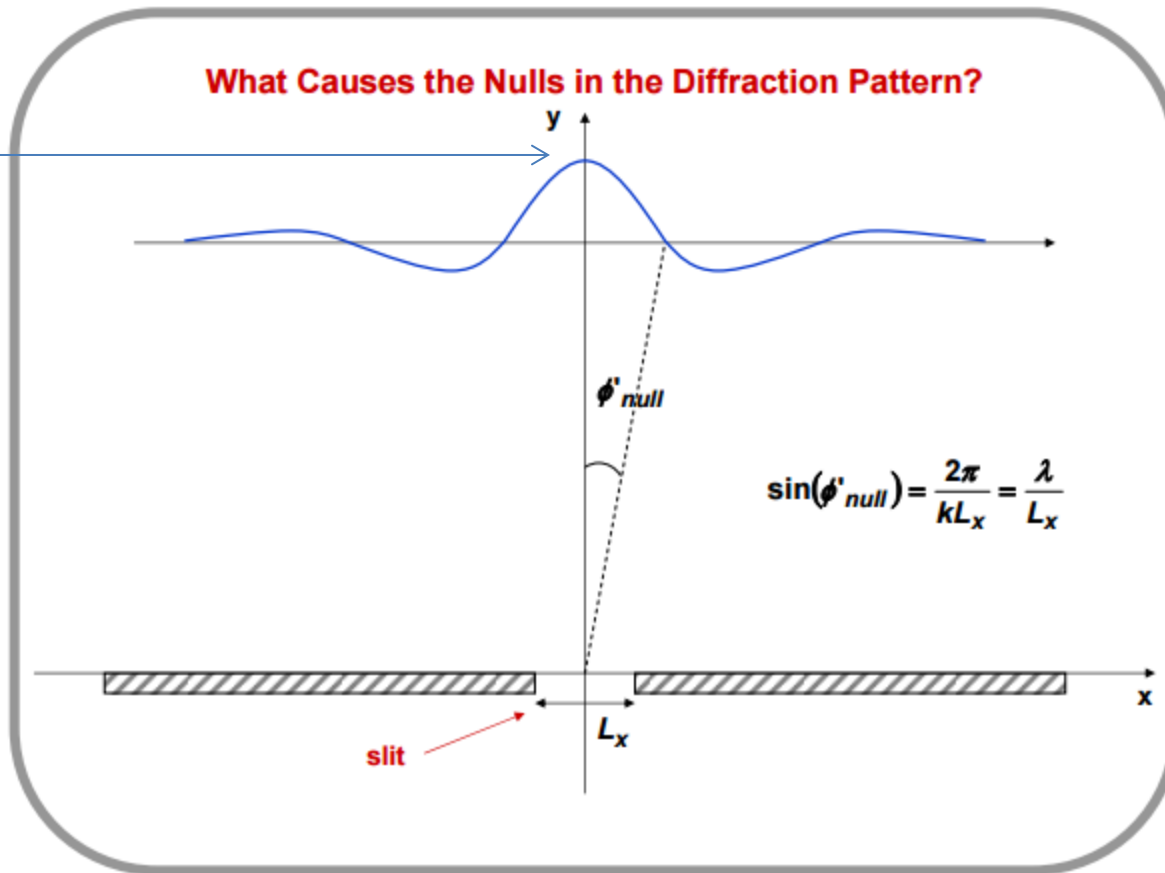
Width of main lobe in k-space =  $\frac{4\pi}{L_x}$

The far-field E-field is proportional to the 2D FT of the aperture shape

$$\begin{aligned} \bar{E}_{ff}(\vec{r}) &= (\hat{\theta}) \frac{j k}{2\pi r} E_a \sin(\theta) e^{-jk r} \int_{-L_x/2}^{L_x/2} e^{jk_x x'} dx' \int_{-L_z/2}^{L_z/2} e^{jk_z z'} dz' \\ &= (\hat{\theta}) \frac{j k}{2\pi r} E_a \sin(\theta) e^{-jk r} (L_x L_z) \frac{\sin(k_x L_x / 2)}{k_x L_x / 2} \frac{\sin(k_z L_z / 2)}{k_z L_z / 2} \end{aligned}$$



Meio: sempre  
maximo pois  
esta tudo em  
fase!

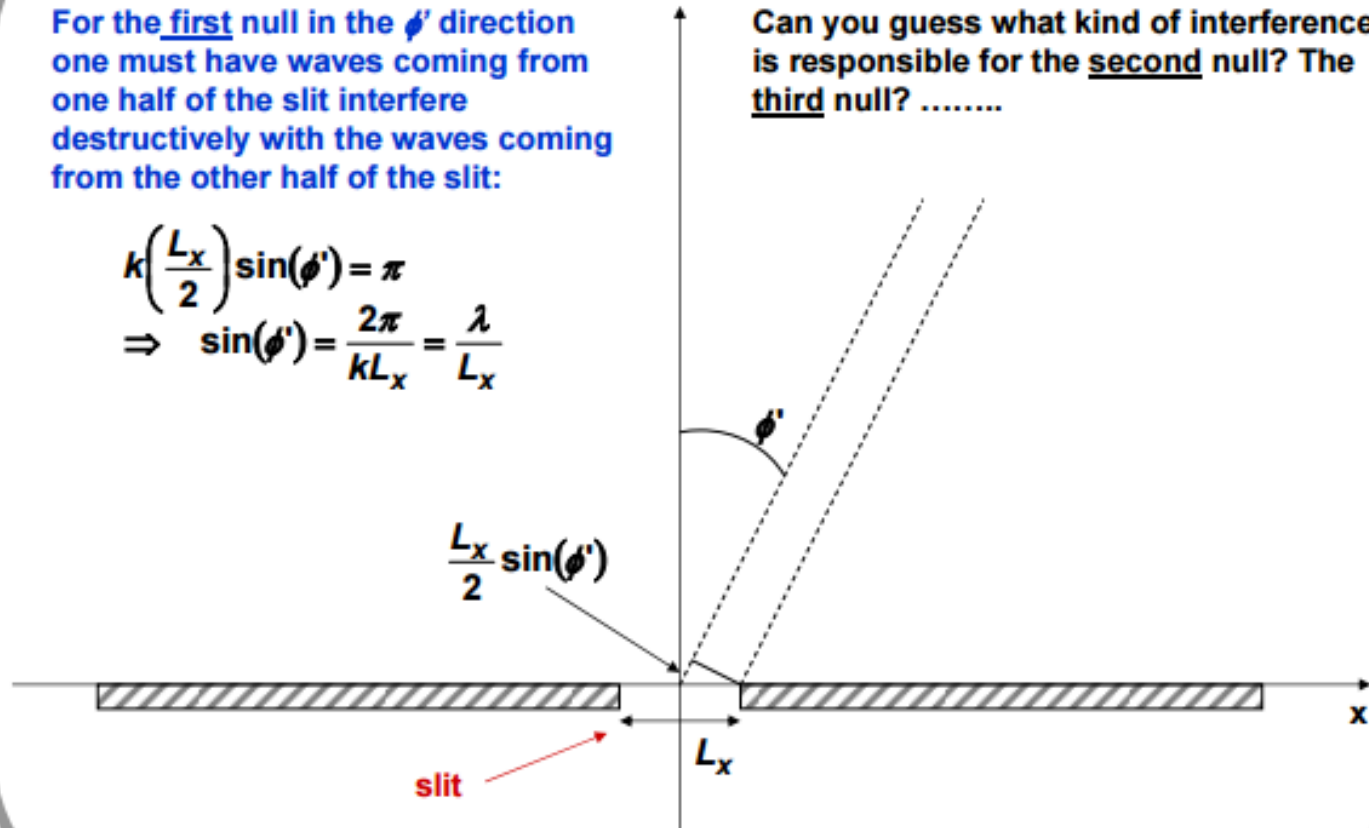


## Nulls in the Diffraction Pattern: Interference in Diffraction

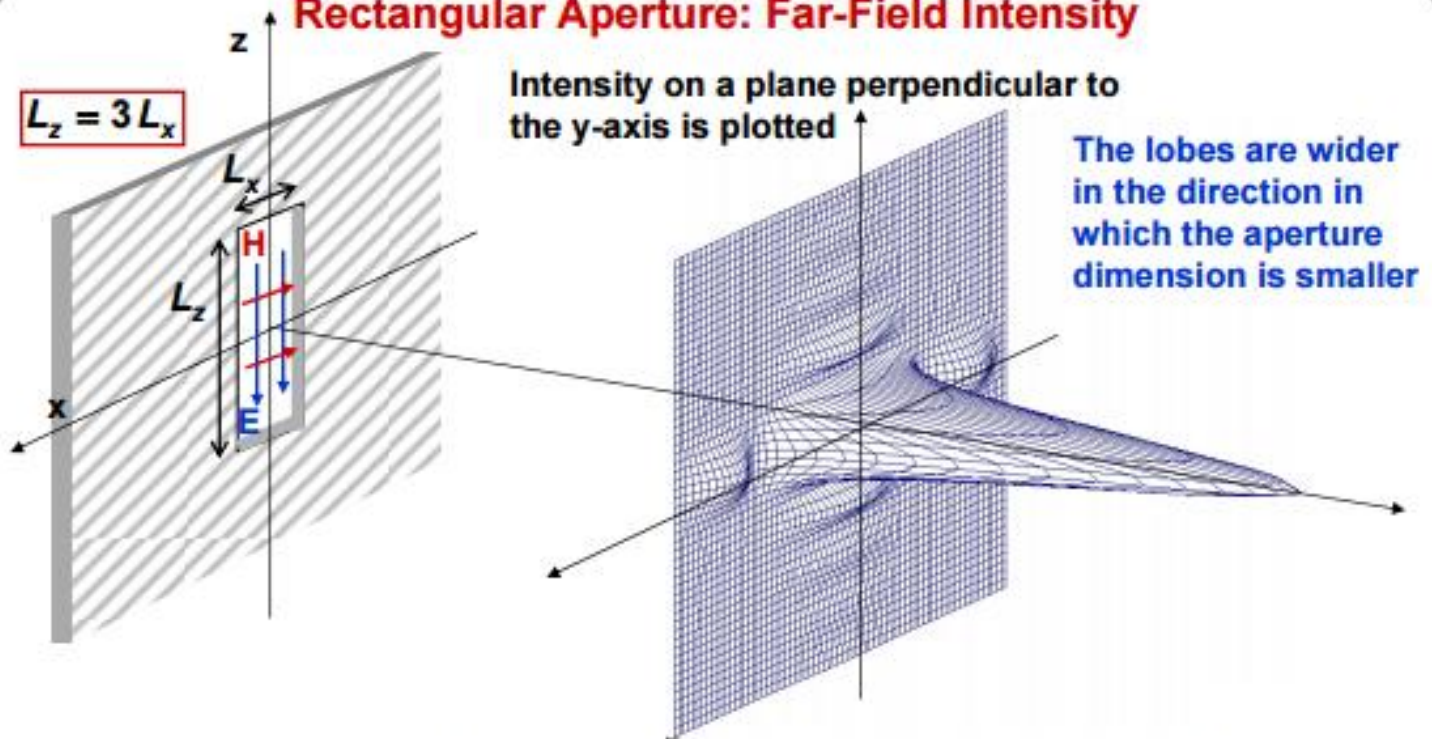
For the first null in the  $\phi'$  direction one must have waves coming from one half of the slit interfere destructively with the waves coming from the other half of the slit:

$$k\left(\frac{L_x}{2}\right)\sin(\phi') = \pi$$
$$\Rightarrow \sin(\phi') = \frac{2\pi}{kL_x} = \frac{\lambda}{L_x}$$

Can you guess what kind of interference is responsible for the second null? The third null? .....



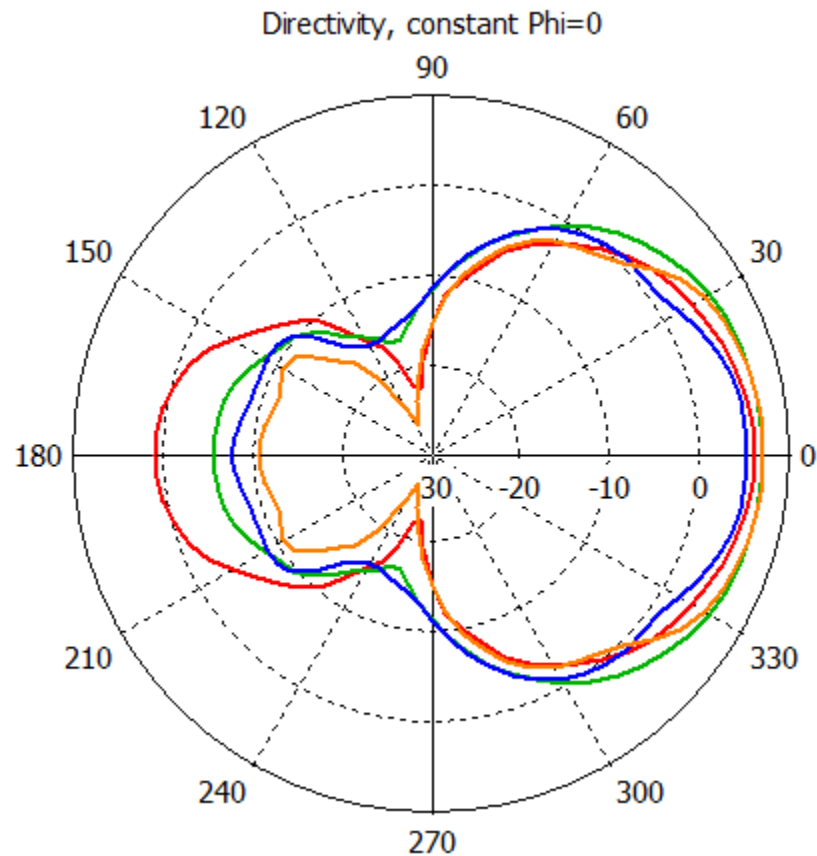
## Rectangular Aperture: Far-Field Intensity



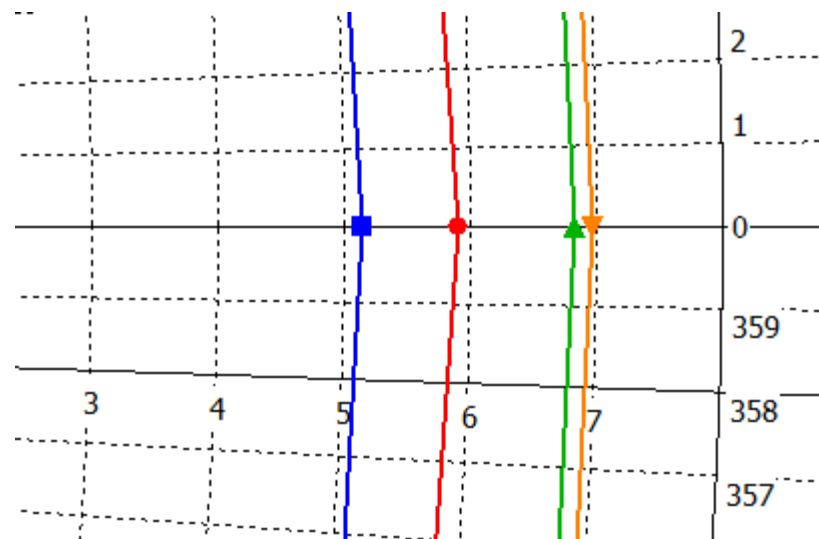
$$\langle \vec{S}_{ff}(\vec{r}, t) \rangle = \hat{r} \frac{1}{2\eta_0} \left| \frac{k E_a}{2\pi r} \right|^2 \sin^2(\theta) \left[ (L_x L_z) \frac{\sin(k_x L_x / 2)}{k_x L_x / 2} \frac{\sin(k_z L_z / 2)}{k_z L_z / 2} \right]^2$$

$$\rightarrow \sin(\theta'_{null}) = \pm \frac{2\pi}{kL_z} = \pm \frac{\lambda}{L_z} \quad \sin(\phi'_{null}) = \pm \frac{2\pi}{kL_x} = \pm \frac{\lambda}{L_x}$$

Obs: aqui dominio continuo (abertura); vale tambem para redes (Ex. 1:5)



- $p=1$
- $p=4$
- $p=7$
- $p=10$

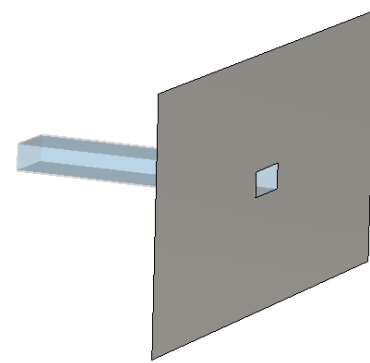
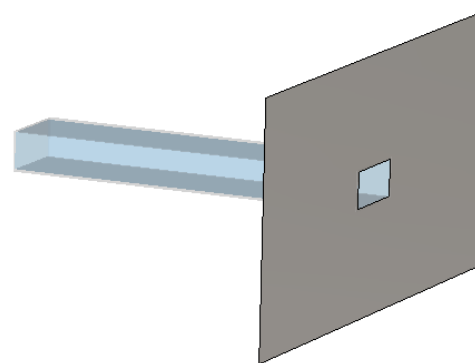
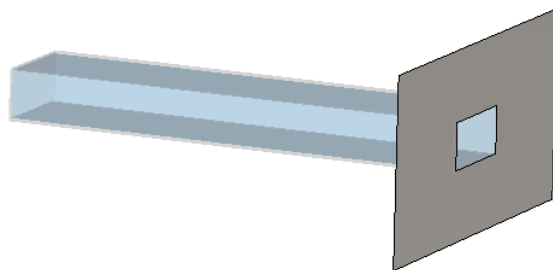
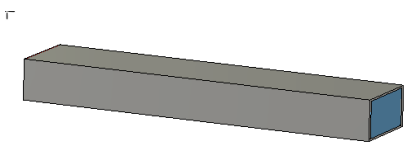


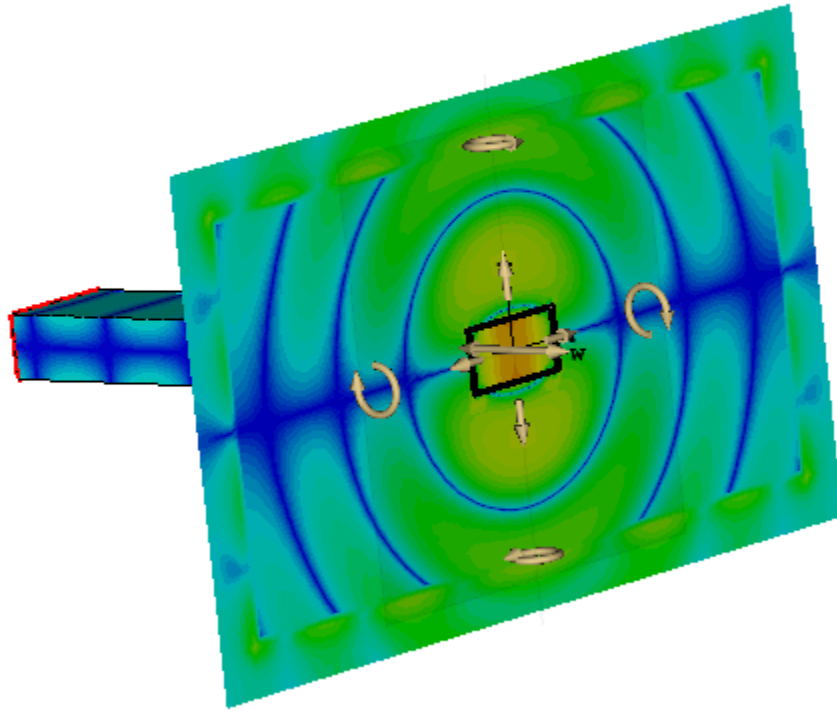
$p=1$

$p=4$

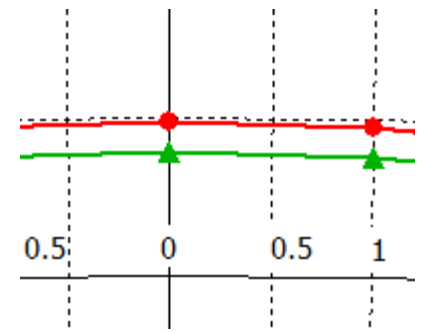
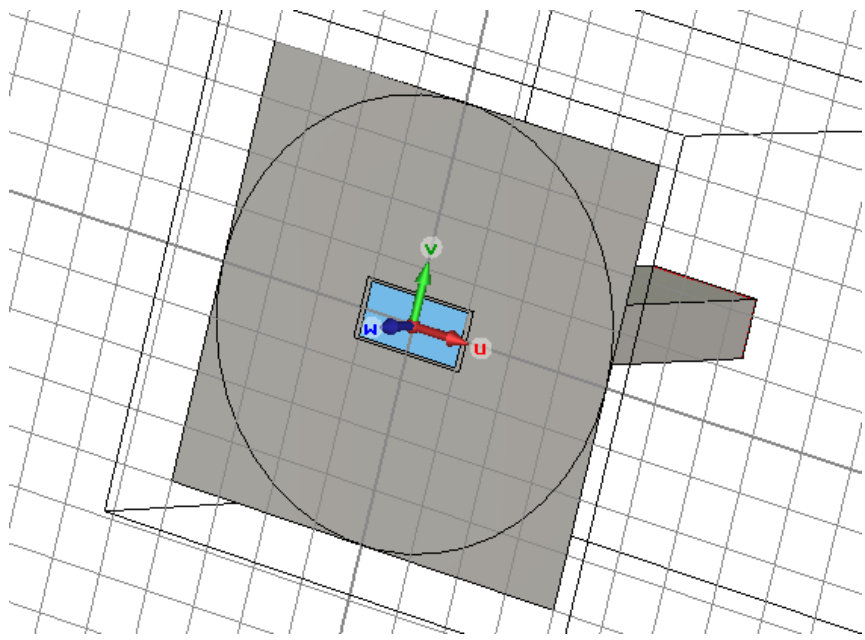
$p=7$

$p=10$



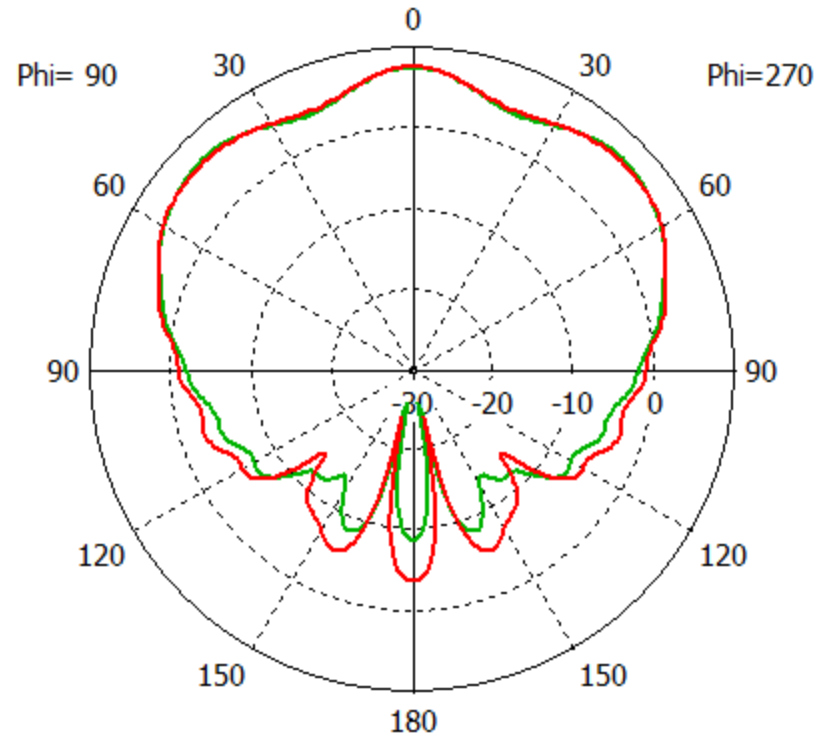


Verifique placa simetria  
retangular mas campos  
circular... E se usarmos  
placa circular?



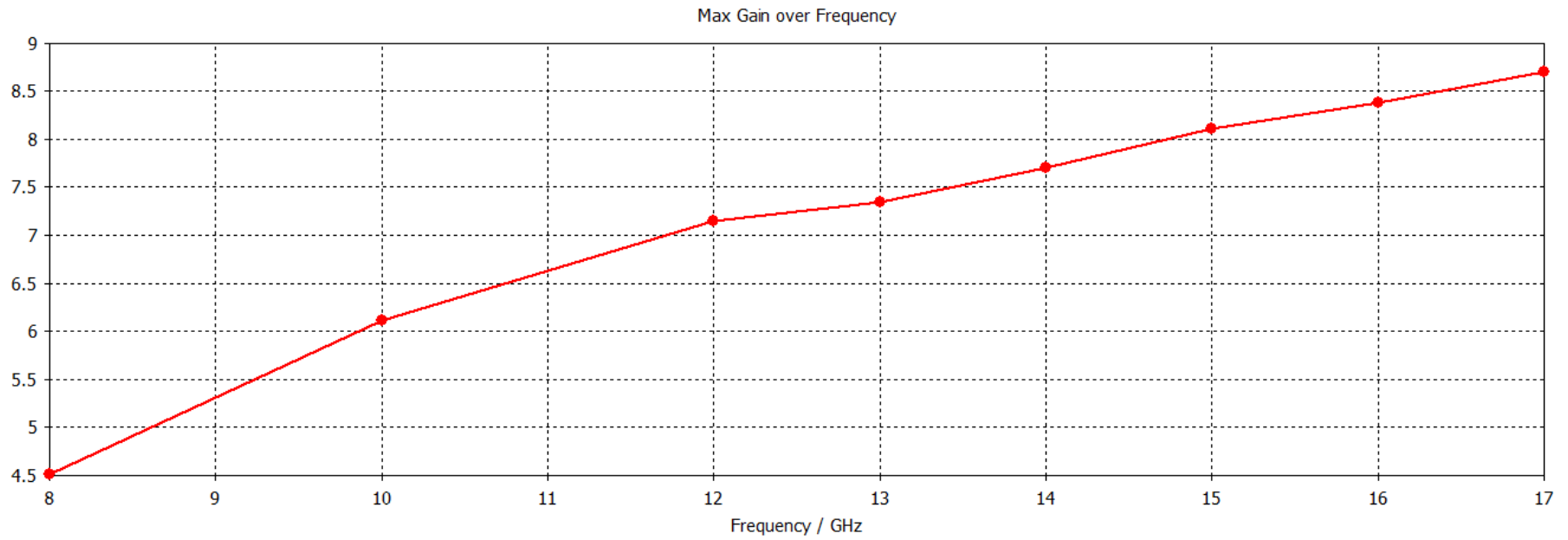
— farfield (f=10) [1]\_cuadrado  
 — farfield (f=10) [1]\_redondo

Farfield Directivity Abs (Phi=90)



Theta / Degree vs. dBi





? Ganho VS. frecuencia aumenta linearmente Por que?