

Parametros S

4.9 A two-port network is driven at both ports such that the port voltages and currents have the following values ($Z_0 = 50 \Omega$):

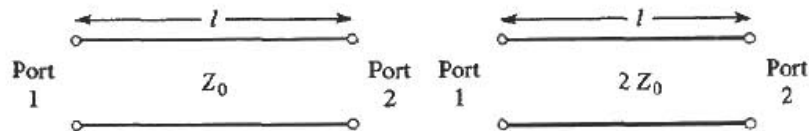
$$\begin{aligned} V_1 &= 20 \angle 0^\circ & I_1 &= 0.4 \angle 90^\circ \\ V_2 &= 4 \angle -90^\circ & I_2 &= 0.08 \angle 0^\circ \end{aligned}$$

Determine the input impedance seen at each port, and find the incident and reflected voltages at each port.

Respostas: $Z_{in}(1) = 50 \angle 90^\circ$ $Z_{in}(2) = 50 \angle -90^\circ$

$V_1^+ = 14.1 \angle 45^\circ$ $V_1^- = 14.1 \angle -45^\circ$ $V_2^+ = 2.82 \angle -45^\circ$ $V_2^- = 2.82 \angle -135^\circ$

4.10 Derive the scattering matrix for each of the lossless transmission lines shown below, relative to a system impedance of Z_0 . Verify that each matrix is unitary.



(a) $S_{22} = S_{11} = 0$ $S_{21} = S_{12} = \exp(-j\beta l)$

(b) $S_{11} = S_{22} = -1/3$ $S_{21} = S_{12} = (8/3) * (\exp(-j\beta l)) / (3 - 0.333 * \exp(-2j\beta l))$

4.11 Consider two two-port networks with individual scattering matrices, $[S^A]$ and $[S^B]$. Show that the overall S_{21} parameter of the cascade of these networks is given by

$$S_{21} = \frac{S_{21}^A S_{21}^B}{1 - S_{22}^A S_{11}^B}$$

4.12 Consider a lossless two-port network. (a) If the network is reciprocal, show that $|S_{21}|^2 = 1 - |S_{11}|^2$. (b) If the network is nonreciprocal, show that it is impossible to have unidirectional transmission, where $S_{12} = 0$ and $S_{21} \neq 0$.

4.15 A certain three-port network is lossless and reciprocal, and has $S_{13} = S_{23}$ and $S_{11} = S_{22}$. Show that if port 2 is terminated with a matched load, then port 1 can be matched by placing an appropriate reactance at port 3.

4.16 A four-port network has the scattering matrix shown below.

- (a) Is this network lossless?
- (b) Is this network reciprocal?
- (c) What is the return loss at port 1 when all other ports are terminated with matched loads?
- (d) What is the insertion loss and phase delay between ports 2 and 4, when all other ports are terminated with matched loads?

$$[S] = \begin{bmatrix} 0.1 \angle 90^\circ & 0.8 \angle -45^\circ & 0.3 \angle -45^\circ & 0 \\ 0.8 \angle -45^\circ & 0 & 0 & 0.4 \angle 45^\circ \\ 0.3 \angle -45^\circ & 0 & 0 & 0.6 \angle -45^\circ \\ 0 & 0.4 \angle 45^\circ & 0.6 \angle -45^\circ & 0 \end{bmatrix}$$

- (e) What is the reflection coefficient seen at port 1 if a short circuit is placed at the terminal plane of port 3, and all other ports are terminated with matched loads?

Respostas: (a) Tem perdas (b) nao reciproca (c) portas 2,3 4 casadas RL=20dB (d) IL=8dB fase 45°

- 4.17 A four-port network has the scattering matrix shown below. If ports 3 and 4 are connected with a lossless matched transmission line with an electrical length of 60°, find the resulting insertion loss and phase delay between ports 1 and 2.

$$[S] = \begin{bmatrix} 0.3 \angle -30^\circ & 0 & 0 & 0.8 \angle 0^\circ \\ 0 & 0.7 \angle -30^\circ & 0.7 \angle -45^\circ & 0 \\ 0 & 0.7 \angle -45^\circ & 0.7 \angle -30^\circ & 0 \\ 0.8 \angle 0^\circ & 0 & 0 & 0.3 \angle -30^\circ \end{bmatrix}$$

Respostas: IL=6.7dB fase 105°

Exemplo 3.17

- (a) Calculate the s -parameters for the two-port network shown in Figure 3.34 for the case where $Z_0 = 50 \Omega$.
- (b) Find the return loss at the input with $Z_L = Z_0$.
- (c) Determine the insertion loss for the network when the generator and the termination are both 50Ω .

Given: Network of Figure 3.34 with $Z_0 = Z_L$.

Required: (a) s -parameters, (b) return loss, (c) insertion loss.

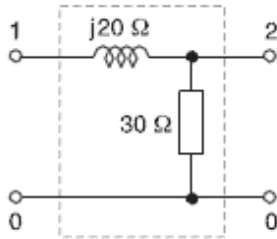


Fig. 3.34 Complex network

Respostas: $s_{11}=0.518 \angle(131.16^\circ)$ $s_{22}=0.442 \angle(172.8^\circ)$ $s_{21}=s_{12}=0.524 \angle(-16.22^\circ)$

Perda retorno = 5.713dB Fwd Pwr Gain = -5.61dB

Example 3.18

A 50Ω microwave integrated circuit (MIC) amplifier has the following s -parameters:

$$\begin{aligned} s_{11} &= 0.12 \angle -10^\circ & s_{12} &= 0.002 \angle -78^\circ \\ s_{21} &= 9.8 \angle 160^\circ & s_{22} &= 0.01 \angle -15^\circ \end{aligned}$$

Calculate: (a) input VSWR, (b) return loss, (c) forward insertion power gain and (d) reverse insertion power loss.

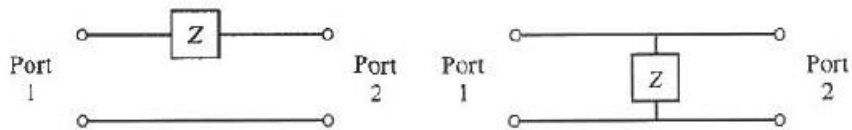
Given: $s_{11} = 0.12 \angle -10^\circ$ $s_{12} = 0.002 \angle -78^\circ$
 $s_{21} = 9.8 \angle 160^\circ$ $s_{22} = 0.01 \angle -15^\circ$

Required: (a) Input VSWR, (b) return loss, (c) forward insertion power gain, (d) reverse insertion power loss.

Respostas: (a) $VSWR = (1+0.12)/(1-0.12)$ (b) $RL=18.42d$ (c) $FWD \text{ Gain}=19.83dB$
 (d) $REV \text{ Gain} = -53.98dB$

Dica: Use a descrição da topologia usando parâmetros ABCD, depois converta usando a tabela para par. S.

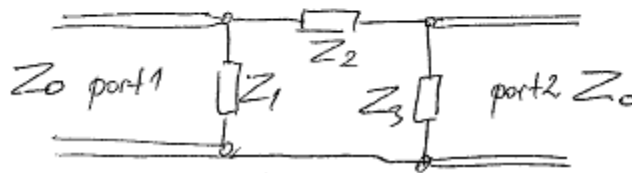
4.28 Find the S parameters for the series and shunt loads shown below. Show that $S_{12} = 1 - S_{11}$ for the series case, and that $S_{12} = 1 + S_{11}$ for the shunt case. Assume a characteristic impedance Z_0 .



Respostas: $S_{11} = Z/(2Z_0 + Z)$ $S_{12} = 2Z_0/(2Z_0 + Z)$ series
 $S_{11} = -Z_0/(Z_0 + 2Z)$ $S_{12} = 2Z/(Z_0 + 2Z)$ shunt

⑤ (Homework)

Express the scattering matrix of the Π -network below in terms of its elements Z_1 , Z_2 , and Z_3 .



Respostas: $S_{11} = Z_{in} - Z_0 / Z_{in} + Z_0$

$Z_{in} = (Z_1 (Z_0 Z_2 + Z_3 Z_2 + Z_0 Z_3)) / (Z_0 Z_1 + Z_3 Z_1 + Z_0 Z_2 + Z_2 Z_3 + Z_0 Z_3)$

$S_{21} = (1 + S_{11}) (Z_0 // Z_3) / ((Z_0 // Z_3) + Z_2)$

Lista Linhas transmissao

3.14 Derive the \vec{E} and \vec{H} fields of a coaxial line from the expression for the potential given in (3.153). Also find expressions for the voltage and current on the line and the characteristic impedance.

Respostas:

$$E(\rho, \phi, z) = V_0 \exp(-j\beta z) / (\rho \ln(b/a)) \text{ na direcao } \rho$$

$$H(\rho, \phi, z) = V_0 \exp(-j\beta z) / (\eta \rho \ln(b/a)) \text{ na direcao } \phi$$

$$V_{ab} = V_0 \exp(-j\beta z)$$

$$I_a = 2\pi V_0 \exp(-j\beta z) / (\eta \ln(b/a))$$

$$Z_0 = \eta \ln(b/a) / 2\pi$$

3.19 Design a stripline transmission line for a 70Ω characteristic impedance. The ground plane separation is 0.316 cm , and the dielectric constant of the filling material is 2.20 . What is the guide wavelength on this transmission line if the frequency is 3.0 GHz ?

Respostas: $w=0.147 \text{ cm}$ e $\lambda_{\text{guiado}}=6.74 \text{ cm}$

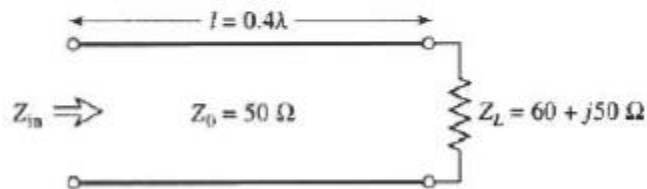
3.20 Design a microstrip transmission line for a 100Ω characteristic impedance. The substrate thickness is 0.158 cm , with $\epsilon_r = 2.20$. What is the guide wavelength on this transmission line if the frequency is 4.0 GHz ?

3.21 A 100Ω microstrip line is printed on a substrate of thickness 0.0762 cm , with a dielectric constant of 2.2 . Ignoring losses and fringing fields, find the shortest length of this line that appears at its input as a capacitor of 5 pF at 2.5 GHz . Repeat for an inductance of 5 nH . Using a microwave CAD package with a physical model for the microstrip line, compute the actual input impedance seen when losses are included (assume copper conductors and $\tan \delta = 0.001$).

Obs. Problema 3.21, deem uma olhada tambem no 2.21 (copia aqui para comodidade).

2.19 Use the Smith chart to find the following quantities for the transmission line circuit below:

- The SWR on the line.
- The reflection coefficient at the load.
- The load admittance.
- The input impedance of the line.
- The distance from the load to the first voltage minimum.
- The distance from the load to the first voltage maximum.



2.20 Repeat problem 2.19 for $Z_L = 40 - j30 \Omega$.

2.21 Repeat problem 2.19 for $l = 1.8\lambda$.

Respostas 3.20 $w=0.142\text{cm}$ $\lambda_{\text{Guiado}}=5.656\text{cm}$ $\epsilon_{\text{eff}}=1.758$

Respostas 3.21 $\beta=3986.7 \text{ }^\circ/\text{m}$ $l=3.2132\text{cm}$

3.22 A microwave antenna feed network operating at 5 GHz requires a 50Ω printed transmission line that is 16λ long. Possible choices are (1) copper microstrip, with $d = 0.16 \text{ cm}$, $\epsilon_r = 2.20$, and $\tan \delta = 0.001$, or (2) copper stripline, with $b = 0.32 \text{ cm}$, $\epsilon_r = 2.20$, $t = 0.01 \text{ mm}$, and $\tan \delta = 0.001$. Which line should be used, if attenuation is to be minimized?

Respostas: Total Loss microlinha = 0.82dB

Total Loss Stripline = 0.91dB

3.28 As discussed in the Point of Interest on the power handling capacity of transmission lines, the maximum power capacity of a coaxial line is limited by voltage breakdown, and is given by

$$P_{\max} = \frac{\pi a^2 E_d^2}{\eta_0} \ln \frac{b}{a}$$

where E_d is the field strength at breakdown. Find the value of b/a that maximizes the maximum power capacity and show that the corresponding characteristic impedance is about 30Ω .

Respostas: $Z_0=30 \text{ Ohms}$

3.A Deseja-se elaborar um sistema para medida de ϵ_r . Para tanto, compute (a) qual a espessura para termos 50 Ohms e (b) qual o comprimento para termos 90 graus - ou $\lambda/4$ – na frequência de 2GHz . O substrato é PCB comum, FR4, com $\epsilon_r=4.6$ e espessura de 40mils .

Respostas: $x=2\text{cm}$

3B. Deseja-se, a partir de um tubo de cobre de 15cm de diâmetro, montar um cabo rígido coaxial de alta potência para broadcast. Calcule:

- o diâmetro do tubo interno para obter 50 Ohms .
- Qual a máxima potência possível de ser transmitida antes de haver um rompimento do dielétrico do ar (centelhamento).
- Obtenha o valor e onde ocorrerá a máxima voltagem no centelhamento.
- Para a frequência de 1KHz , qual seria a espessura mínima que teríamos que especificar a parede dos tubos? Pense em termos de *skin depth effect* (efeito pelicular).

Respostas: (a) 6.52cm (b) 28MW (c) 35.4kV (d) $\delta=2\text{mm}$ interessante manter aprox. 3δ de espessura

3Ca. Um cabo coaxial transmite DC? Como voce faria uma conexão de uma bateria num cabo coaxial para transporte de corrente contínua?

3Cb. Repita a questão anterior para o guia de onda. Justifique.

3C. Um técnico pergunta por que ele ligou o multímetro, escala de resistências, em um cabo coaxial em aberto (vermelho no inner e preto na malha) e não observou 50 Ohms. Como você explicaria a ele em termos simples?

3D. Deseja-se substituir um sistema *lumped* (com componente, ou concentrada) com um indutor de 5nH, na frequência de 1GHz. (a) Aponte qual a estrutura que será usada (stub curto ou aberto?), desenhando o final e com a dimensão da microlinha de 50 Ohms usada (espessura e comprimento). Use o substrato usado no exercício 3A. (b) Qual seria o inconveniente, baseado na sua resposta, dessa montagem distribuída em relação a concentrada? (c) O que seria possível de prever, em função da disciplina EMC, do uso da solução distribuída?

Respostas: stub em curto; $w=1.87\text{mm}$ $\epsilon_{\text{eff}}=3.45$ comprimento $l=0.82\text{m}$