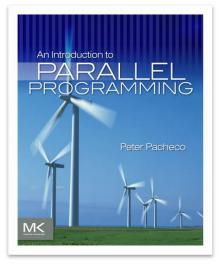


An Introduction to Parallel Programming

Peter Pacheco



#### Chapter 3

Distributed Memory Programming with MPI

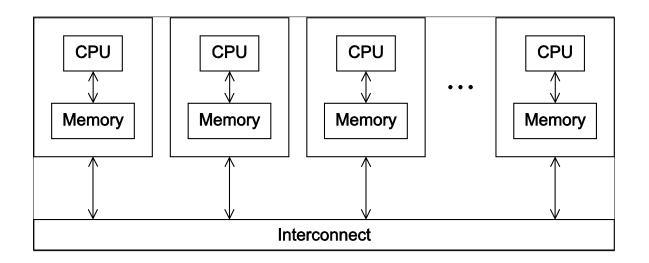


# Roadmap

- Writing your first MPI program.
- Using the common MPI functions.
- The Trapezoidal Rule in MPI.
- Collective communication.
- MPI derived datatypes.
- Performance evaluation of MPI programs.
- Parallel sorting.
- Safety in MPI programs.

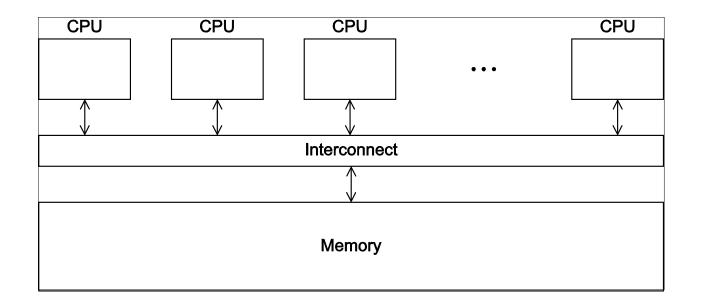


# A distributed memory system





# A shared memory system





# Hello World!

```
#include <stdio.h>
```

```
int main(void) {
    printf("hello, world\n");
```

```
return 0;
```

ł



#### (a classic)



# **Identifying MPI processes**

- Common practice to identify processes by nonnegative integer ranks.
- processes are numbered 0, 1, 2, ... p-1



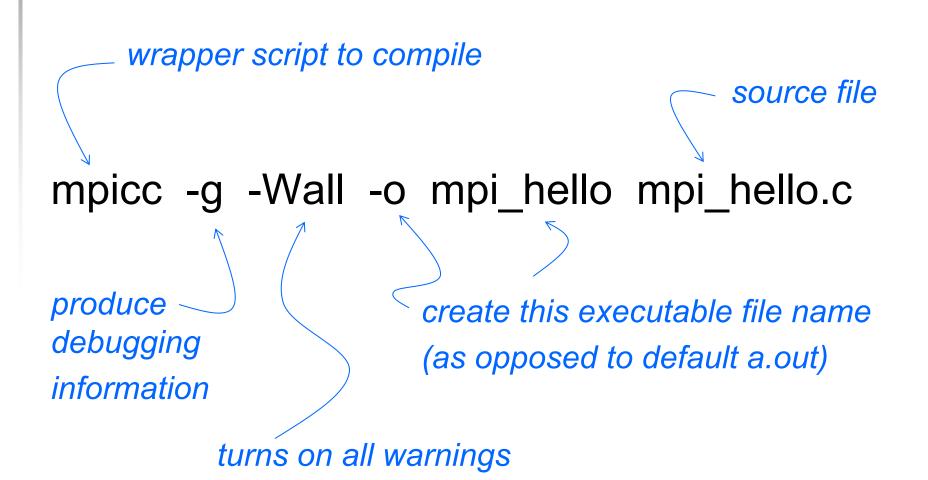
# **Our first MPI program**

```
1 #include <stdio.h>
  #include <string.h> /* For strlen
2
                                                    */
3 #include <mpi.h> /* For MPI functions, etc */
4
   const int MAX_STRING = 100;
5
6
7
   int main(void) {
8
                 greeting [MAX STRING]:
      char
             comm_sz; /* Number of processes */
9
      int
               my_rank; /* My process rank
10
      int
                                                    */
11
12
      MPI Init(NULL, NULL);
13
      MPI Comm size (MPI COMM WORLD, &comm sz):
      MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
14
15
      if (my_rank != 0) {
16
         sprintf(greeting, "Greetings from process %d of %d!",
17
18
               my rank, comm sz);
19
         MPI_Send(greeting, strlen(greeting)+1, MPI_CHAR, 0, 0,
20
               MPI COMM WORLD);
21
      } else {
22
         printf("Greetings from process %d of %d!\n", my_rank, comm_sz);
23
         for (int q = 1; q < comm_sz; q++) {
24
            MPI_Recv(greeting, MAX_STRING, MPI_CHAR, q,
25
               0, MPI COMM WORLD, MPI STATUS IGNORE);
26
            printf("%s\n", greeting);
27
28
      }
29
30
      MPI Finalize();
31
      return 0;
32
      /* main */
```



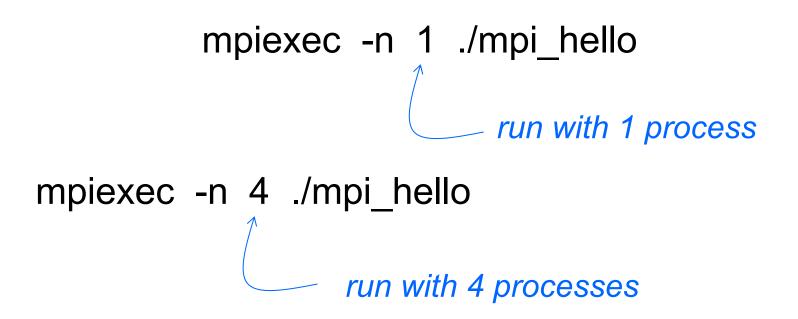


# **Compilation**





#### mpiexec -n <number of processes> <executable>







mpiexec -n 1 ./mpi\_hello

Greetings from process 0 of 1 !

mpiexec -n 4 ./mpi\_hello

Greetings from process 0 of 4 !

Greetings from process 1 of 4 !

Greetings from process 2 of 4 !

Greetings from process 3 of 4 !



# **MPI Programs**

- Written in C.
  - Has main.
  - Uses stdio.h, string.h, etc.
- Need to add mpi.h header file.
- Identifiers defined by MPI start with "MPI\_".
- First letter following underscore is uppercase.
  - For function names and MPI-defined types.
  - Helps to avoid confusion.



# **MPI Components**

#### MPI\_Init

Tells MPI to do all the necessary setup.

int MPI\_Init(
 int\* argc\_p /\* in/out \*/,
 char\*\*\* argv\_p /\* in/out \*/);

#### MPI\_Finalize

 Tells MPI we're done, so clean up anything allocated for this program.

int MPI\_Finalize(void);



# **Basic Outline**

```
NEN 22 1723
#include <mpi.h>
int main(int argc, char* argv[]) {
   9 C (9)
   /* No MPI calls before this */
   MPI_Init(&argc, &argv);
   4.7 (2.4)
   MPI_Finalize();
   /* No MPI calls after this */
   return 0;
```



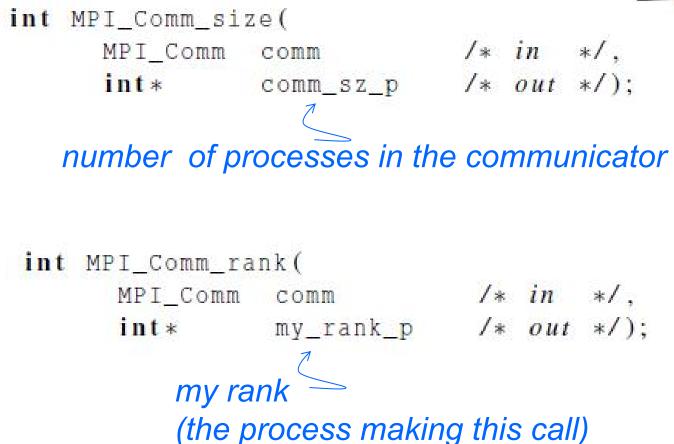
# **Communicators**

- A collection of processes that can send messages to each other.
- MPI\_Init defines a communicator that consists of all the processes created when the program is started.
- Called MPI\_COMM\_WORLD.



# Communicators







# **SPMD**

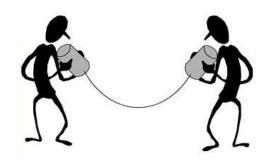
- Single-Program Multiple-Data
- We compile <u>one</u> program.
- Process 0 does something different.
  - Receives messages and prints them while the other processes do the work.
- The if-else construct makes our program SPMD.



# Communication

#### int MPI\_Send(

msg_buf_p	/*	in	*/,
msg_size	/*	in	*/,
msg_type	/*	in	*/,
dest	/*	in	*/,
tag	/*	in	*/,
communicator	/*	in	*/);
	msg_size msg_type dest tag	msg_size /* msg_type /* dest /* tag /*	msg_size /* in msg_type /* in dest /* in





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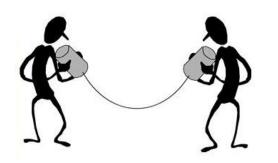
# Data types

MPI datatype	C datatype
MPI_CHAR	signed char
MPI_SHORT	signed short int
MPI_INT	signed int
MPI_LONG	signed long int
MPI_LONG_LONG	signed long long int
MPI_UNSIGNED_CHAR	unsigned char
MPI_UNSIGNED_SHORT	unsigned short int
MPI_UNSIGNED	unsigned int
MPI_UNSIGNED_LONG	unsigned long int
MPI_FLOAT	float
MPI_DOUBLE	double
MPI_LONG_DOUBLE	long double
MPI_BYTE	
MPI_PACKED	



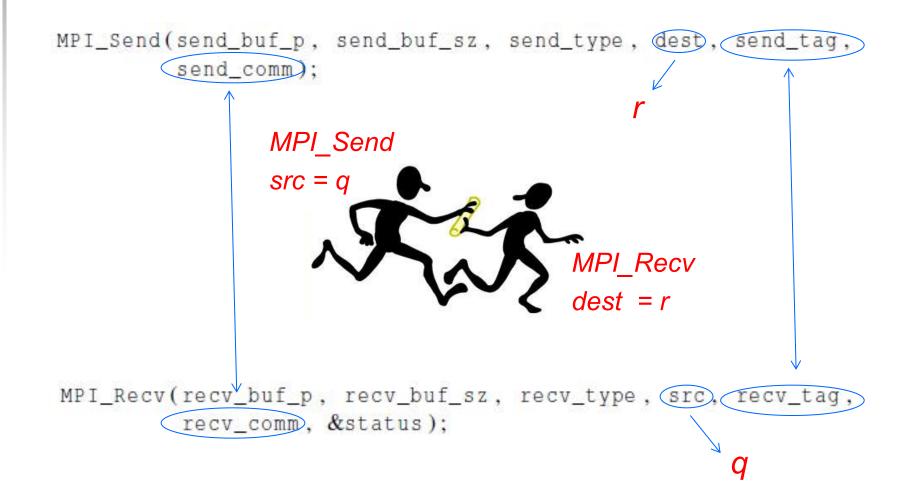
# Communication

void *	msg_buf_p	/*	out	*/,
int	buf_size	/*	in	*/,
MPI_Datatype	buf_type	/*	in	*/,
int	source	/*	in	*/,
int	tag	/*	in	*/,
MPI_Comm	communicator	/*	in	*/,
MPI_Status*	status_p	/*	out	*/):





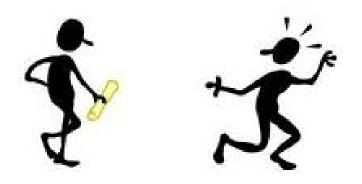
## **Message matching**





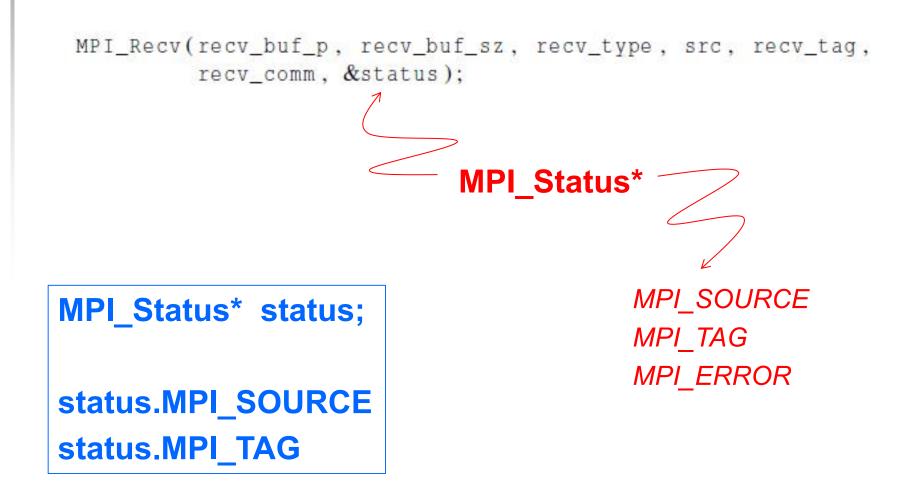
# **Receiving messages**

- A receiver can get a message without knowing:
  - the amount of data in the message,
  - the sender of the message,
  - or the tag of the message.





# status\_p argument





# How much data am I receiving?

# int MPI\_Get\_count( MPI\_Status\* status\_p /\* in \*/, MPI\_Datatype type /\* in \*/, int\* count\_p /\* out \*/);



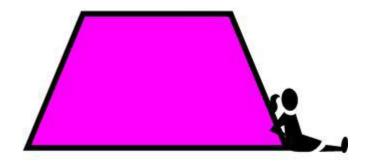


## **Issues with send and receive**

- Exact behavior is determined by the MPI implementation.
- MPI\_Send may behave differently with regard to buffer size, cutoffs and blocking.
- MPI\_Recv always blocks until a matching message is received.
- Know your implementation; don't make assumptions!





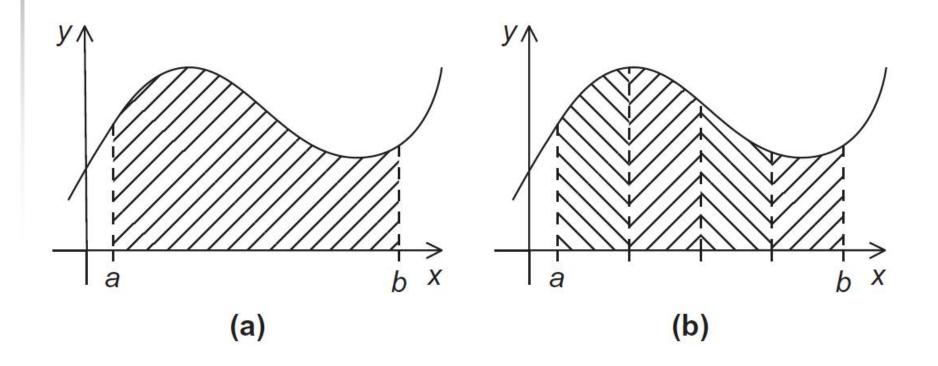


# **TRAPEZOIDAL RULE IN MPI**



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#### **The Trapezoidal Rule**





#### **The Trapezoidal Rule**

Area of one trapezoid 
$$= \frac{h}{2}[f(x_i) + f(x_{i+1})]$$

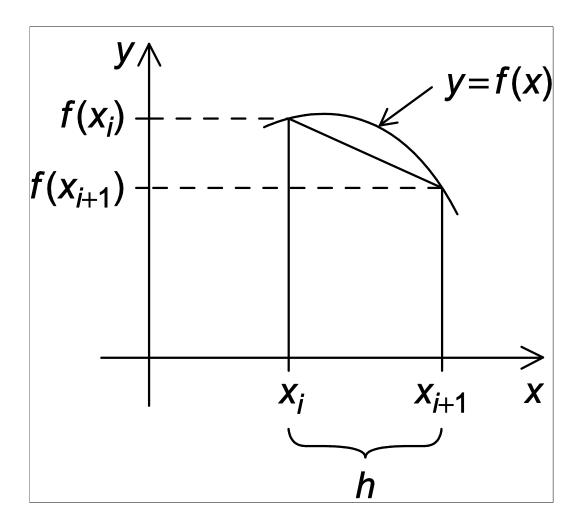
$$h = \frac{b-a}{n}$$

$$x_0 = a, x_1 = a + h, x_2 = a + 2h, \dots, x_{n-1} = a + (n-1)h, x_n = b$$

Sum of trapezoid areas  $= h[f(x_0)/2 + f(x_1) + f(x_2) + \dots + f(x_{n-1}) + f(x_n)/2]$ 



## **One trapezoid**





# Pseudo-code for a serial

#### program

```
/* Input: a, b, n */
h = (b-a)/n:
approx = (f(a) + f(b))/2.0;
for (i = 1; i \le n-1; i++) {
   x_i = a + i_{*h}:
   approx += f(x_i);
approx = h*approx;
```



# **Parallelizing the Trapezoidal Rule**

- 1. Partition problem solution into tasks.
- 2. Identify communication channels between tasks.
- 3. Aggregate tasks into composite tasks.
- 4. Map composite tasks to cores.

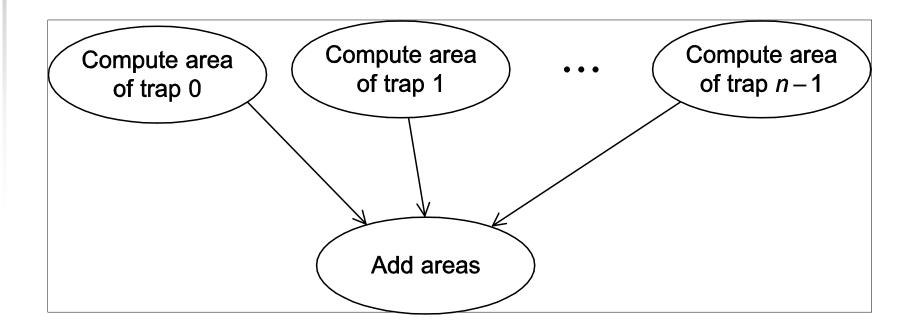


## **Parallel pseudo-code**

```
1
      Get a, b, n;
2
      h = (b-a)/n;
3
      local n = n/comm sz;
      local_a = a + my_rank*local_n*h;
4
5
      local_b = local_a + local_n*h;
6
      local_integral = Trap(local_a, local_b, local_n, h);
7
      if (my rank != 0)
8
         Send local_integral to process 0;
9
      else /* my_rank == 0 */
10
         total integral = local integral;
11
         for (proc = 1; proc < comm_sz; proc++) {</pre>
12
             Receive local integral from proc;
13
            total_integral += local_integral;
14
15
16
      if (my rank == 0)
17
         print result;
```



# Tasks and communications for Trapezoidal Rule





# First version (1)

```
int main(void) {
 1
2
      int my rank, comm sz, n = 1024, local n;
3
      double a = 0.0, b = 3.0, h, local a, local b;
4
      double local int, total int;
5
      int source:
6
7
      MPI Init(NULL, NULL);
8
      MPI Comm rank(MPI COMM WORLD, & my rank);
9
      MPI Comm size (MPI COMM WORLD, &comm sz);
10
11
      h = (b-a)/n; /* h is the same for all processes */
      local_n = n/comm_sz; /* So is the number of trapezoids */
12
13
14
      local a = a + my rank*local n*h;
15
      local b = local a + local n*h;
16
      local int = Trap(local a, local b, local n, h);
17
18
      if (my rank != 0) {
         MPI_Send(&local_int, 1, MPI_DOUBLE, 0, 0,
19
20
               MPI COMM WORLD);
```



# First version (2)

```
21
      } else {
22
         total int = local int;
23
         for (source = 1; source < comm sz; source++) {</pre>
24
             MPI Recv(&local int, 1, MPI DOUBLE, source, 0,
25
                   MPI COMM WORLD, MPI STATUS IGNORE);
26
             total int += local int;
27
28
29
30
      if (my rank == 0) {
31
         printf("With n = %d trapezoids, our estimate\n", n);
32
         printf("of the integral from %f to %f = %.15e\n",
33
              a, b, total int);
34
35
      MPI Finalize();
36
      return 0:
37
     /* main */
```



# First version (3)

```
double Trap(
 1
2
         double left_endpt /* in */,
3
         double right endpt /* in */,
4
         int trap_count /* in */,
5
         double base_len /* in */) {
6
      double estimate, x;
7
      int i:
8
9
      estimate = (f(left endpt) + f(right endpt))/2.0;
10
      for (i = 1; i \le trap_count - 1; i++)
11
         x = left endpt + i*base len;
12
         estimate += f(x);
13
      }
14
      estimate = estimate*base len;
15
16
      return estimate;
     /* Trap */
17
```



# **Dealing with I/O**

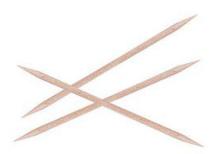
```
#include <stdio.h>
#include <mpi.h>
                                  Each process just
                                  prints a message.
int main(void) {
   int my rank, comm sz;
   MPI Init(NULL, NULL);
   MPI Comm size (MPI COMM WORLD, & comm sz);
   MPI Comm rank (MPI COMM WORLD, &my rank);
   printf("Proc %d of %d > Does anyone have a toothpick?\n",
         my rank, comm sz);
   MPI Finalize();
   return 0;
   /* main */
```



#### **Running with 6 processes**

Proc 0 of 6 > Does anyone have a toothpick? Proc 1 of 6 > Does anyone have a toothpick? Proc 2 of 6 > Does anyone have a toothpick? Proc 4 of 6 > Does anyone have a toothpick? Proc 3 of 6 > Does anyone have a toothpick? Proc 5 of 6 > Does anyone have a toothpick?

unpredictable output





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#### Input

 Most MPI implementations only allow process 0 in MPI\_COMM\_WORLD access to stdin.

Process 0 must read the data (scanf) and send to the other processes.

```
MPI_Comm_rank(MPI_COMM_WORLD, &my_rank);
MPI_Comm_size(MPI_COMM_WORLD, &comm_sz);
Get_data(my_rank, comm_sz, &a, &b, &n);
h = (b-a)/n;
. . .
```



## **Function for reading user input**

```
void Get_input(
     int my rank /* in */.
     int comm_sz /* in */,
     double* a_p /* out */,
     double* b_p /* out */,
     int* np /* out */) {
  int dest;
  if (my_rank == 0) {
     printf("Enter a, b, and n\n");
     scanf("%lf %lf %d", a p, b p, n p);
     for (dest = 1; dest < comm sz; dest++) {</pre>
        MPI_Send(a_p, 1, MPI_DOUBLE, dest, 0, MPI_COMM_WORLD);
        MPI_Send(b_p, 1, MPI_DOUBLE, dest, 0, MPI_COMM_WORLD);
        MPI Send(n p, 1, MPI INT, dest, 0, MPI COMM WORLD);
  else \{ /* my_rank != 0 */
     MPI_Recv(a_p, 1, MPI_DOUBLE, 0, 0, MPI COMM WORLD.
           MPI STATUS IGNORE);
     MPI_Recv(b_p, 1, MPI_DOUBLE, 0, 0, MPI_COMM_WORLD,
           MPI_STATUS_IGNORE);
     MPI_Recv(n_p, 1, MPI_INT, 0, 0, MPI_COMM_WORLD.
           MPI STATUS IGNORE);
  /* Get_input */
```



# COLLECTIVE COMMUNICATION





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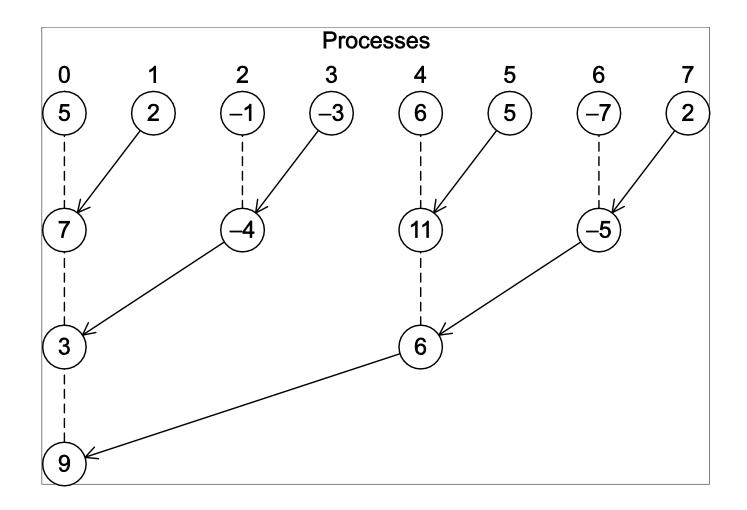
#### **Tree-structured communication**

- In the first phase:

   (a) Process 1 sends to 0, 3 sends to 2, 5 sends to 4, and 7 sends to 6.
   (b) Processes 0, 2, 4, and 6 add in the received values.
   (c) Processes 2 and 6 send their new values to processes 0 and 4, respectively.
   (d) Processes 0 and 4 add the received values into their new values.
- 2. (a) Process 4 sends its newest value to process 0.(b) Process 0 adds the received value to its newest value.

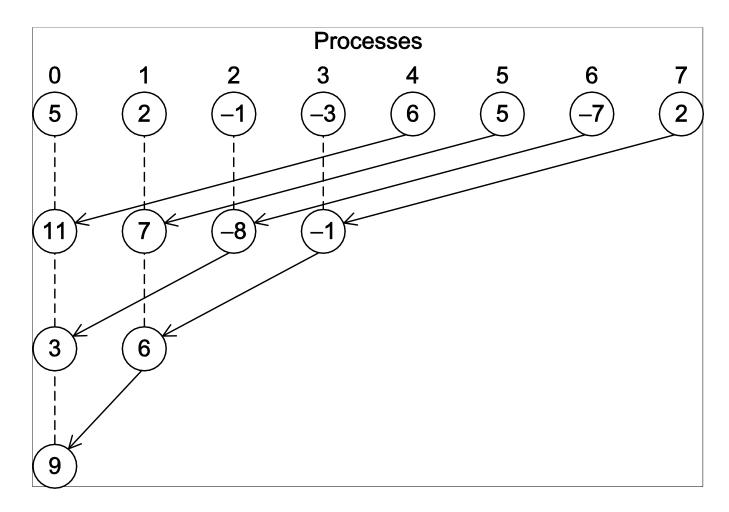


#### A tree-structured global sum





# An alternative tree-structured global sum





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# **MPI\_Reduce**

void *	input_data_p	/*	in	*/,
void *	output_data_p	/*	out	*/,
int	count	/*	in	*/,
MPI_Datatype	datatype	/*	in	*/,
MPI_Op	operator	/*	in	*/,
int	dest_process	/*	in	*/,
MPI_Comm	comm	/*	in	*/)



# **Predefined reduction operators**

# in MPI

Operation Value	Meaning
MPI_MAX	Maximum
MPI_MIN	Minimum
MPI_SUM	Sum
MPI_PROD	Product
MPI_LAND	Logical and
MPI_BAND	Bitwise and
MPI_LOR	Logical or
MPI_BOR	Bitwise or
MPI_LXOR	Logical exclusive or
MPI_BXOR	Bitwise exclusive or
MPI_MAXLOC	Maximum and location of maximum
MPI_MINLOC	Minimum and location of minimum



All the processes in the communicator must call the same collective function.

For example, a program that attempts to match a call to MPI\_Reduce on one process with a call to MPI\_Recv on another process is erroneous, and, in all likelihood, the program will hang or crash.



- The arguments passed by each process to an MPI collective communication must be "compatible."
- For example, if one process passes in 0 as the dest\_process and another passes in 1, then the outcome of a call to MPI\_Reduce is erroneous, and, once again, the program is likely to hang or crash.



The output\_data\_p argument is only used on dest\_process.

However, all of the processes still need to pass in an actual argument corresponding to output\_data\_p, even if it's just NULL.



- Point-to-point communications are matched on the basis of tags and communicators.
- Collective communications don't use tags.
   They're matched solely on the basis of the communicator and the order in which they're called.



## Example (1)

Time	Process 0	Process 1	Process 2		
0	a = 1; c = 2	a = 1; c = 2	a = 1; c = 2		
1	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)		
2	MPI_Reduce(&c, &d,)	MPI_Reduce(&a, &b,)	MPI_Reduce(&c, &d,)		

#### Multiple calls to MPI\_Reduce



 Suppose that each process calls MPI\_Reduce with operator MPI\_SUM, and destination process 0.

At first glance, it might seem that after the two calls to MPI\_Reduce, the value of b will be 3, and the value of d will be 6.



 However, the names of the memory locations are irrelevant to the matching of the calls to MPI\_Reduce.

The order of the calls will determine the matching so the value stored in b will be 1+2+1 = 4, and the value stored in d will be 2+1+2 = 5.

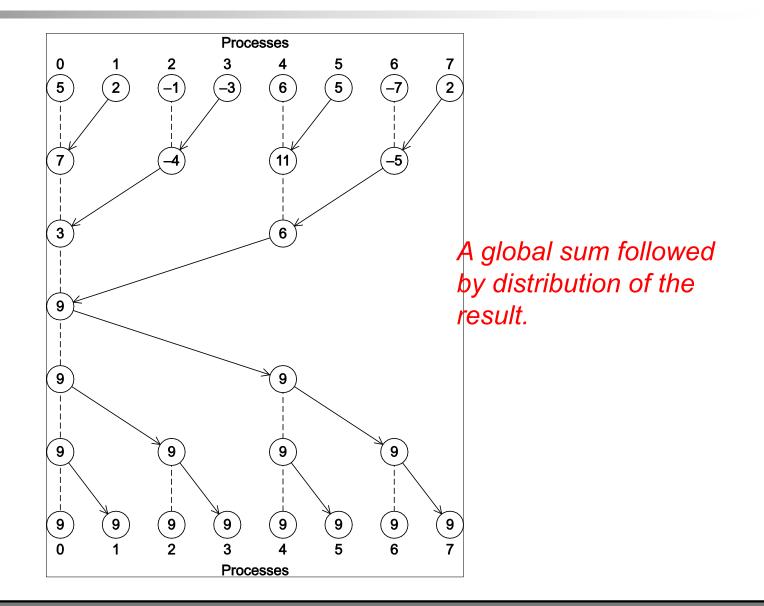


# **MPI\_Allreduce**

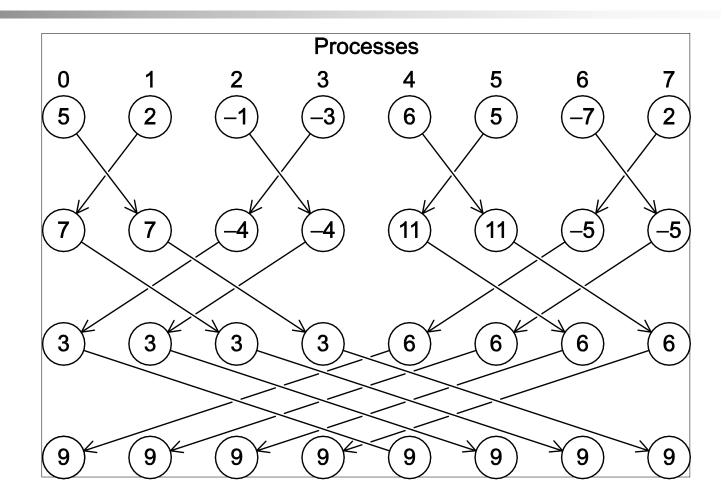
 Useful in a situation in which all of the processes need the result of a global sum in order to complete some larger computation.

```
int MPI_Allreduce(
         void *
                      input_data_p /* in
                                           */,
                      output_data_p /* out */,
         void *
                                  /* in */.
         int
                     count
                                    /* in */,
        MPI_Datatype datatype
                                    /* in */.
        MPI_Op
                     operator
                                     /* in */);
        MPI Comm
                     COMM
```









A butterfly-structured global sum.



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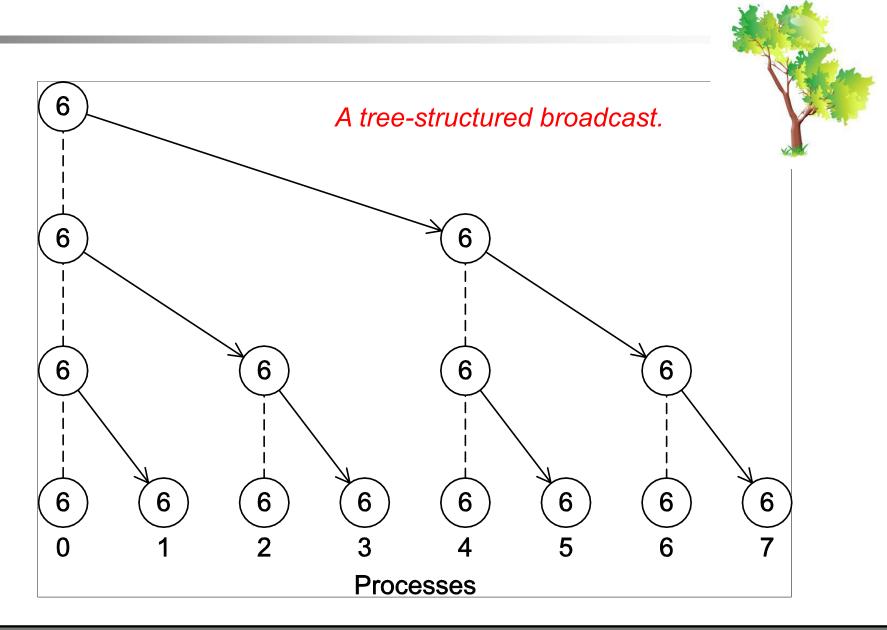


#### **Broadcast**

 Data belonging to a single process is sent to all of the processes in the communicator.

int MPI_Bcast(				
void *	data_p	/*	in/out	*/,
int	count	/*	in	*/,
MPI_Datatype	datatype	/*	in	*/,
int	source_proc	/*	in	*/,
MPI_Comm	comm	/*	in	*/);







# A version of Get\_input that uses MPI\_Bcast

void Get\_input(
 int my\_rank /\* in \*/,
 int comm\_sz /\* in \*/,
 double\* a\_p /\* out \*/,
 double\* b\_p /\* out \*/,
 int\* n\_p /\* out \*/) {

```
if (my_rank == 0) {
    printf("Enter a, b, and n\n");
    scanf("%lf %lf %d", a_p, b_p, n_p);
}
MPI_Bcast(a_p, 1, MPI_DOUBLE, 0, MPI_COMM_WORLD);
MPI_Bcast(b_p, 1, MPI_DOUBLE, 0, MPI_COMM_WORLD);
MPI_Bcast(n_p, 1, MPI_INT, 0, MPI_COMM_WORLD);
/* Get_input */
```



#### **Data distributions**

#### $\mathbf{x} + \mathbf{y} = (x_0, x_1, \dots, x_{n-1}) + (y_0, y_1, \dots, y_{n-1})$ $= (x_0 + y_0, x_1 + y_1, \dots, x_{n-1} + y_{n-1})$ $= (z_0, z_1, \dots, z_{n-1})$ $= \mathbf{z}$

Compute a vector sum.



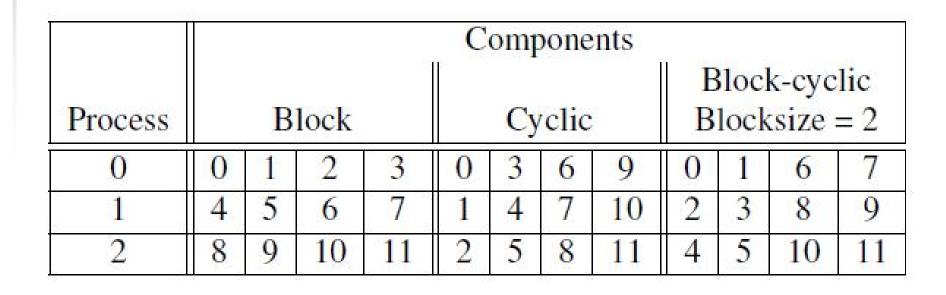
# Serial implementation of vector addition

void Vector\_sum(double x[], double y[], double z[], int n) {
 int i;

for (i = 0; i < n; i++)
 z[i] = x[i] + y[i];
/\* Vector\_sum \*/</pre>



# Different partitions of a 12component vector among 3 processes





# **Partitioning options**

- Block partitioning
  - Assign blocks of consecutive components to each process.
- Cyclic partitioning
  - Assign components in a round robin fashion.
- Block-cyclic partitioning
  - Use a cyclic distribution of blocks of components.



# Parallel implementation of vector addition

```
void Parallel_vector_sum(
    double local_x[] /* in */,
    double local_y[] /* in */,
    double local_z[] /* out */,
    int local_n /* in */) {
    int local_i;
    for (local_i = 0; local_i < local_n; local_i++)
        local_z[local_i] = local_x[local_i] + local_y[local_i];
} /* Parallel_vector_sum */</pre>
```



#### **Scatter**

MPI\_Scatter can be used in a function that reads in an entire vector on process 0 but only sends the needed components to each of the other processes.

<pre>int MPI_Scatter(</pre>				
void *	send_buf_p	/*	in	*/,
int	send_count	/*	in	*/,
MPI_Dataty	pe send_type	/*	in	*/,
void *	recv_buf_p	/*	out	*/,
int	recv_count	/*	in	*/,
MPI_Dataty	pe recv_type	/*	i n	*/,
int	src_proc	/*	in	*/,
MPI_Comm	comm	/*	in	*/);



## **Reading and distributing a vector**

```
void Read vector(
     double local_a[] /* out */,
     int local n /* in */,
                    /* in */.
     int
             n
     char vec name[] /* in */,
     int my_rank /* in */.
     MPI_Comm comm /* in */) {
  double * a = NULL;
  int i:
  if (my rank == 0) {
     a = malloc(n*sizeof(double));
     printf("Enter the vector %s\n", vec name);
     for (i = 0; i < n; i++)
        scanf("%lf", &a[i]);
     MPI Scatter(a, local n, MPI DOUBLE, local a, local n, MPI DOUBLE,
          0, comm);
     free(a);
  } else {
     MPI Scatter(a, local n, MPI DOUBLE, local a, local n, MPI DOUBLE,
           0. comm);
  /* Read_vector */
```



#### Gather

 Collect all of the components of the vector onto process 0, and then process 0 can process all of the components.

int	MPI_Gather(				
	void *	<pre>send_buf_p</pre>	/*	in	*/,
	int	send_count	/*	in	*/,
	MPI_Datatype	send_type	/*	in	*/,
	void *	recv_buf_p	/*	out	*/,
	int	recv_count	/*	in	*/,
	MPI_Datatype	recv_type	/*	in	*/,
	int	dest_proc	/*	in	*/,
	MPI_Comm	comm	/*	in	*/);



## **Print a distributed vector (1)**

#### void Print\_vector(

double	local_b[]	/*	i n	*/,
int	local_n	/*	i n	*/,
int	n	/*	in	*/,
char	title[]	/*	i n	*/,
int	my_rank	/*	i n	*/,
MPI_Comm	comm	/*	i n	*/) {

double \* b = NULL; int i;



## Print a distributed vector (2)

```
if (my rank == 0) {
  b = malloc(n*sizeof(double));
  MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE,
         0. comm):
  printf("%s\n", title);
  for (i = 0; i < n; i++)
     printf("%f ", b[i]);
  printf("\n");
  free(b);
} else {
  MPI_Gather(local_b, local_n, MPI_DOUBLE, b, local_n, MPI_DOUBLE,
         0, comm);
/* Print_vector */
```



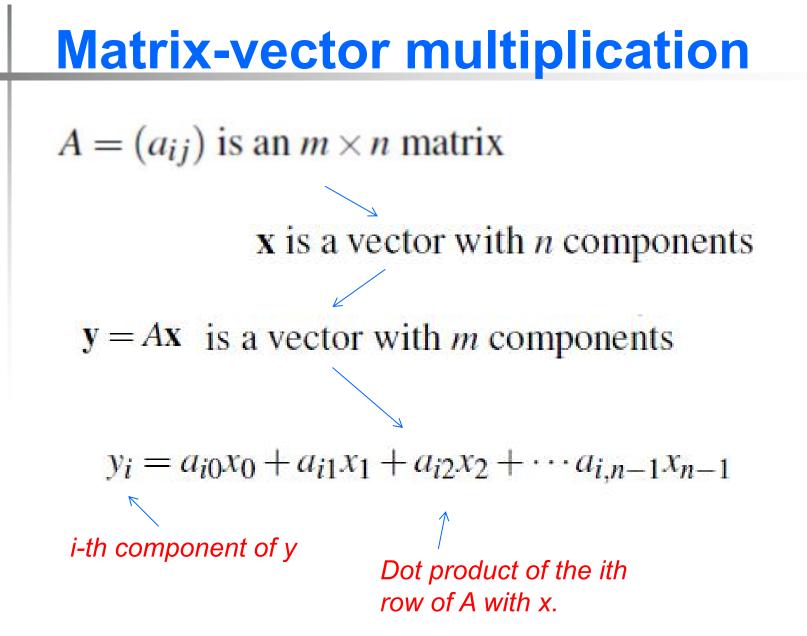
## Allgather

Concatenates the contents of each process' send\_buf\_p and stores this in each process' recv\_buf\_p.

As usual, recv\_count is the amount of data being received from each process.

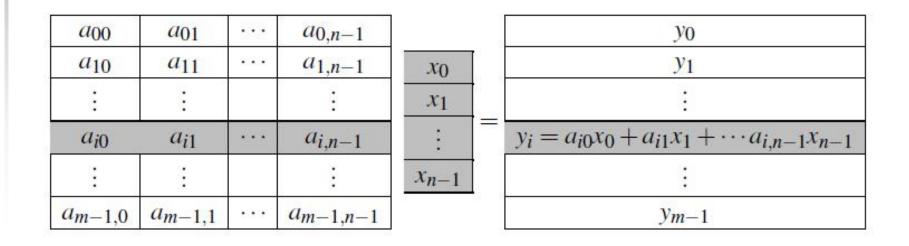
int	MPI_Allgather(				
	void *	<pre>send_buf_p</pre>	/*	in	*/,
	int	send_count	/*	in	*/,
	MPI_Datatype	<pre>send_type</pre>	/*	in	*/,
	void *	recv_buf_p	/*	out	*/,
	int	recv_count	/*	i n	*/,
	MPI_Datatype	recv_type	/*	i n	*/,
	MPI_Comm	comm	/*	in	*/);







#### **Matrix-vector multiplication**





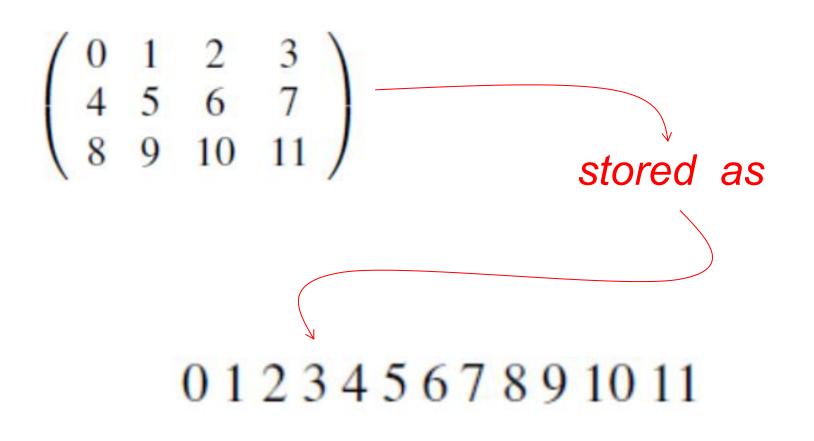
## Multiply a matrix by a vector

/\* For each row of A \*/
for (i = 0; i < m; i++) {
 /\* Form dot product of ith row with x \*/
 v[i] = 0.0;
 for (j = 0; j < n; j++)
 y[i] += A[i][j]\*x[j];
}</pre>

Serial pseudo-code



### **C** style arrays





# Serial matrix-vector multiplication

void Mat\_vect\_mult( double A[] /\* in \*/, double x[] /\* in \*/, **double** y[] /\* out \*/, int m /\* in \*/, int n /\* in \*/) { int i, j; for (i = 0; i < m; i++) { v[i] = 0.0;for (j = 0; j < n; j++)y[i] += A[i\*n+j]\*x[j];}
/\* Mat\_vect\_mult \*/



## An MPI matrix-vector multiplication function (1)

void Mat_vect_mu	ilt(			
double	local_A[]	/*	in	*/,
double	local_x[]	/*	in	*/,
double	local_y[]	/*	out	*/,
int	local_m	/*	i n	*/,
int	n	/*	in	*/,
int	local_n	/*	in	*/,
MPI_Comm	comm	/*	i n	*/) {
double * x;				
<pre>int local_i,</pre>	j;			
<pre>int local_ok</pre>	= 1;			



# An MPI matrix-vector multiplication function (2)

```
for (local_i = 0; local_i < local_m; local_i++) {
    local_y[local_i] = 0.0;
    for (j = 0; j < n; j++)
        local_y[local_i] += local_A[local_i*n+j]*x[j];
}
free(x);
/* Mat_vect_mult */</pre>
```





## **MPI DERIVED DATATYPES**



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#### **Derived datatypes**

- Used to represent any collection of data items in memory by storing both the types of the items and their relative locations in memory.
- The idea is that if a function that sends data knows this information about a collection of data items, it can collect the items from memory before they are sent.
- Similarly, a function that receives data can distribute the items into their correct destinations in memory when they're received.



#### **Derived datatypes**

 Formally, consists of a sequence of basic MPI data types together with a displacement for each of the data types.

Trapezoidal Rule example:

Variable	Address
a	24
b	40
n	48

 $\{(MPI_DOUBLE, 0), (MPI_DOUBLE, 16), (MPI_INT, 24)\}$ 



## **MPI\_Type create\_struct**

 Builds a derived datatype that consists of individual elements that have different basic types.

<pre>int MPI_Type_create_</pre>	struct(			
int	count	/*	in	*/,
int	array_of_blocklengths[]	/*	in	*/,
MPI_Aint	array_of_displacements[]	/*	in	*/,
MPI_Datatype	<pre>array_of_types[]</pre>	/*	in	*/,
MPI_Datatype*	new_type_p	/*	out	*/);



## **MPI\_Get\_address**

- Returns the address of the memory location referenced by location\_p.
- The special type MPI\_Aint is an integer type that is big enough to store an address on the system.

int MPI\_Get\_address(
 void \* location\_p /\* in \*/,
 MPI\_Aint\* address\_p /\* out \*/);



# MPI\_Type\_commit

 Allows the MPI implementation to optimize its internal representation of the datatype for use in communication functions.

int MPI\_Type\_commit(MPI\_Datatype\* new\_mpi\_t\_p /\* in/out \*/);



# **MPI\_Type\_free**

When we're finished with our new type, this frees any additional storage used.

int MPI\_Type\_free(MPI\_Datatype\* old\_mpi\_t\_p /\* in/out \*/);



# Get input function with a derived datatype (1)

void	<pre>Build_mpi_type(</pre>				
	double *	a_p	/*	in	*/,
	double *	b_p	/*	in	*/,
	int *	n_p	/*	in	*/,
	MPI_Datatype*	<pre>input_mpi_t_p</pre>	/*	out	*/) {

```
int array_of_blocklengths[3] = {1, 1, 1};
MPI_Datatype array_of_types[3] = {MPI_DOUBLE, MPI_DOUBLE, MPI_INT};
MPI_Aint a_addr, b_addr, n_addr;
MPI_Aint array_of_displacements[3] = {0};
```



# Get input function with a derived datatype (2)

```
MPI_Get_address(a_p, &a_addr);
MPI_Get_address(b_p, &b_addr);
MPI_Get_address(n_p, &n_addr);
array_of_displacements[1] = b_addr-a_addr;
array_of_displacements[2] = n_addr-a_addr;
MPI_Type_create_struct(3, array_of_blocklengths,
array_of_displacements, array_of_types,
input_mpi_t_p);
MPI_Type_commit(input_mpi_t_p);
/* Build_mpi_type */
```



# Get input function with a derived datatype (3)

Build\_mpi\_type(a\_p, b\_p, n\_p, &input\_mpi\_t);

```
if (my_rank == 0) {
    printf("Enter a, b, and n\n");
    scanf("%lf %lf %d", a_p, b_p, n_p);
}
MPI_Bcast(a_p, 1, input_mpi_t, 0, MPI_COMM_WORLD);
MPI_Type_free(&input_mpi_t);
/* Get_input */
```





## **PERFORMANCE EVALUATION**



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### **Elapsed parallel time**

Returns the number of seconds that have elapsed since some time in the past.



### **Elapsed serial time**

- In this case, you don't need to link in the MPI libraries.
- Returns time in microseconds elapsed from some point in the past.

```
#include "timer.h"
. . .
double now;
. . .
GET TIME(now);
```





#### **Elapsed serial time**

```
#include "timer.h"
. . .
double start, finish;
. . .
GET_TIME(start);
/* Code to be timed */
. . .
GET_TIME(finish);
printf("Elapsed time = %e seconds\n", finish-start);
```



## **MPI\_Barrier**

Ensures that no process will return from calling it until every process in the communicator has started calling it.

int MPI\_Barrier(MPI\_Comm comm /\* in \*/);





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## **MPI\_Barrier**

```
double local_start, local_finish, local_elapsed, elapsed;
. . .
MPI Barrier(comm);
local start = MPI Wtime();
/* Code to be timed */
· · ·
local finish = MPI Wtime();
local elapsed = local finish - local_start;
MPI_Reduce(&local_elapsed, &elapsed, 1, MPI_DOUBLE,
  MPI MAX, 0, comm);
if (my rank == 0)
   printf("Elapsed time = %e seconds\n", elapsed);
```



## **Run-times of serial and parallel matrix-vector multiplication**

	Order of Matrix				
comm_sz	1024	2048	4096	8192	16,384
1	4.1	16.0	64.0	270	1100
2	2.3	8.5	33.0	140	560
4	2.0	5.1	18.0	70	280
8	1.7	3.3	9.8	36	140
16	1.7	2.6	5.9	19	71

(Seconds)



## Speedup

$$S(n,p) = \frac{T_{\text{serial}}(n)}{T_{\text{parallel}}(n,p)}$$



### Efficiency

$$E(n,p) = \frac{S(n,p)}{p} = \frac{T_{\text{serial}}(n)}{p \times T_{\text{parallel}}(n,p)}$$



## **Speedups of Parallel Matrix-Vector Multiplication**

comm_sz	1024	2048	4096	8192	16,384
1	1.0	1.0	1.0	1.0	1.0
2	1.8	1.9	1.9	1.9	2.0
4	2.1	3.1	3.6	3.9	3.9
8	2.4	4.8	6.5	7.5	7.9
16	2.4	6.2	10.8	14.2	15.5



## **Efficiencies of Parallel Matrix-Vector Multiplication**

2	Order of Matrix					
comm_sz	1024	2048	4096	8192	16,384	
1	1.00	1.00	1.00	1.00	1.00	
2	0.89	0.94	0.97	0.96	0.98	
4	0.51	0.78	0.89	0.96	0.98	
8	0.30	0.61	0.82	0.94	0.98	
16	0.15	0.39	0.68	0.89	0.97	



### **Scalability**

A program is scalable if the problem size can be increased at a rate so that the efficiency doesn't decrease as the number of processes increase.





### **Scalability**

Programs that can maintain a constant efficiency without increasing the problem size are sometimes said to be strongly scalable.

Programs that can maintain a constant efficiency if the problem size increases at the same rate as the number of processes are sometimes said to be weakly scalable.



## A PARALLEL SORTING ALGORITHM



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## Sorting

- n keys and p = comm sz processes.
- n/p keys assigned to each process.
- No restrictions on which keys are assigned to which processes.
- When the algorithm terminates:
  - The keys assigned to each process should be sorted in (say) increasing order.
  - If 0 ≤ q < r < p, then each key assigned to process q should be less than or equal to every key assigned to process r.



### Serial bubble sort

```
void Bubble_sort(
     int a[] /* in/out */,
     int n /* in */) {
  int list_length, i, temp;
  for (list_length = n; list_length >= 2; list_length--)
     for (i = 0; i < list_length - 1; i++)
        if (a[i] > a[i+1]) {
           temp = a[i];
           a[i] = a[i+1];
           a[i+1] = temp;
```

} /\* Bubble\_sort \*/



### **Odd-even transposition sort**

 A sequence of phases.
 Even phases, compare swaps: (a[0],a[1]),(a[2],a[3]),(a[4],a[5]),...
 Odd phases, compare swaps:

 $(a[1], a[2]), (a[3], a[4]), (a[5], a[6]), \ldots$ 



#### Example

Start: 5, 9, 4, 3 Even phase: compare-swap (5,9) and (4,3) getting the list 5, 9, 3, 4 Odd phase: compare-swap (9,3) getting the list 5, 3, 9, 4 Even phase: compare-swap (5,3) and (9,4) getting the list 3, 5, 4, 9 Odd phase: compare-swap (5,4) getting the list 3, 4, 5, 9



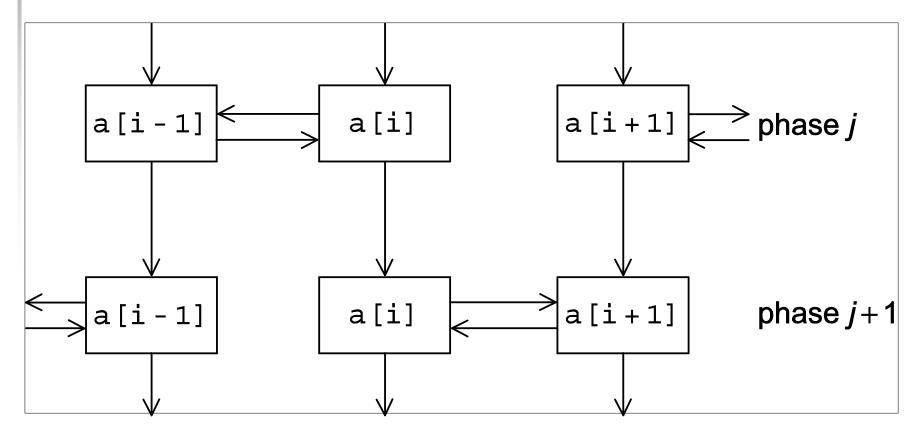
## **Serial odd-even transposition**

sort

```
void Odd_even_sort(
      int a [] /* in/out */,
      int n /* in */) {
   int phase, i, temp;
  for (phase = 0; phase < n; phase++)
      if (phase % 2 == 0) { /* Even phase */
         for (i = 1; i < n; i += 2)
            if (a[i-1] > a[i]) {
              temp = a[i];
               a[i] = a[i-1];
              a[i-1] = temp;
      } else { /* Odd phase */
         for (i = 1; i < n-1; i += 2)
            if (a[i] > a[i+1]) {
               temp = a[i];
               a[i] = a[i+1];
               a[i+1] = temp;
  /* Odd_even_sort */
```



# Communications among tasks in odd-even sort



Tasks determining a[i] are labeled with a[i].



## **Parallel odd-even transposition**

#### sort

	Process						
Time	0	1	2	3			
Start	15, 11, 9, 16	3, 14, 8, 7	4, 6, 12, 10	5, 2, 13, 1			
After Local Sort	9, 11, 15, 16	3, 7, 8, 14	4, 6, 10, 12	1, 2, 5, 13			
After Phase 0	3, 7, 8, 9	11, 14, 15, 16	1, 2, 4, 5	6, 10, 12, 13			
After Phase 1	3, 7, 8, 9	1, 2, 4, 5	11, 14, 15, 16	6, 10, 12, 13			
After Phase 2	1, 2, 3, 4	5, 7, 8, 9	6, 10, 11, 12	13, 14, 15, 16			
After Phase 3	1, 2, 3, 4	5, 6, 7, 8	9, 10, 11, 12	13, 14, 15, 16			



#### **Pseudo-code**

```
Sort local keys;
for (phase = 0; phase < comm_sz; phase++) {</pre>
   partner = Compute_partner(phase, my_rank);
   if (I'm not idle) {
      Send my keys to partner;
      Receive keys from partner;
      if (my_rank < partner)
         Keep smaller keys;
      else
         Keep larger keys;
```



# **Compute\_partner**

if (phase % 2 == 0) /\* Even phase \*/ if (my\_rank % 2 != 0) /\* Odd rank \*/ partner =  $my_rank - 1;$ else /\* Even rank \*/ partner = my rank + 1; else /\* Odd phase \*/ if (my\_rank % 2 != 0) /\* Odd rank \*/ partner =  $my_rank + 1;$ /\* Even rank \*/ else partner =  $my_rank - 1$ ; if (partner == -1 || partner == comm\_sz) partner = MPI\_PROC\_NULL;



- The MPI standard allows MPI\_Send to behave in two different ways:
  - it can simply copy the message into an MPI managed buffer and return,
  - or it can block until the matching call to MPI\_Recv starts.



- Many implementations of MPI set a threshold at which the system switches from buffering to blocking.
- Relatively small messages will be buffered by MPI\_Send.
- Larger messages, will cause it to block.



If the MPI\_Send executed by each process blocks, no process will be able to start executing a call to MPI\_Recv, and the program will hang or deadlock.

Each process is blocked waiting for an event that will never happen.

(see pseudo-code)



A program that relies on MPI provided buffering is said to be unsafe.

Such a program may run without problems for various sets of input, but it may hang or crash with other sets.



### **MPI\_Ssend**

An alternative to MPI\_Send defined by the MPI standard.

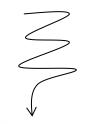
The extra "s" stands for synchronous and MPI\_Ssend is guaranteed to block until the matching receive starts.

int	MPI_Ssend(				
	void *	msg_buf_p	/*	in	*/,
	int	msg_size	/*	i n	*/,
	MPI_Datatype	msg_type	/*	in	*/,
	int	dest	/*	in	*/,
	int	tag	/*	in	*/,
	MPI_Comm	communicator	/*	in	*/);



#### **Restructuring communication**

MPI\_Send(msg, size, MPI\_INT, (my\_rank+1) % comm\_sz, 0, comm); MPI\_Recv(new\_msg, size, MPI\_INT, (my\_rank+comm\_sz-1) % comm\_sz, 0, comm, MPI\_STATUS\_IGNORE.





# **MPI\_Sendrecv**

- An alternative to scheduling the communications ourselves.
- Carries out a blocking send and a receive in a single call.
- The dest and the source can be the same or different.
- Especially useful because MPI schedules the communications so that the program won't hang or crash.



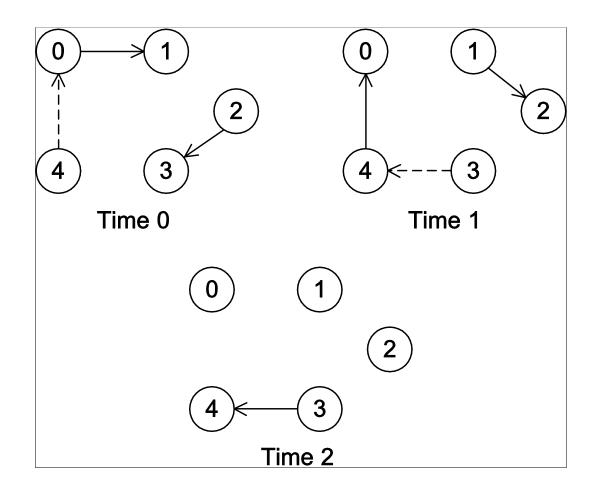
# **MPI\_Sendrecv**

<pre>int MPI_Sendrecv(</pre>				
void *	send_buf_p	/*	in	* <b>/</b> ,
int	<pre>send_buf_size</pre>	/*	in	*/,
MPI_Datatype	<pre>send_buf_type</pre>	/*	in	*/,
int	dest	/*	in	*/,
int	send_tag	/*	i n	*/,
void *	recv_buf_p	/*	<mark>out</mark>	*/,
int	recv_buf_size	/*	in	*/,
MPI_Datatype	recv_buf_type	/*	in	* <b>/</b> ,
int	source	/*	in	*/,
int	recv_tag	/*	in	* <b>/</b> ,
MPI_Comm	communicator	/*	in	*/,
MPI_Status*	status_p	/*	in	* <b>/</b> );



## Safe communication with five

#### processes





#### Parallel odd-even transposition sort

```
void Merge low(
     int my_keys[], /* in/out */
     int recv_keys[], /* in */
     int temp_keys[], /* scratch */
     int local_n /* = n/p, in */ {
  int mi, ri, ti;
  mi = ri = ti = 0;
  while (t_i < local_n) {</pre>
     if (my_keys[m_i] <= recv_keys[r_i]) {</pre>
        temp_keys[t_i] = my_keys[m_i];
       t i++; m i++;
     } else {
        temp_keys[t_i] = recv_keys[r_i];
       t_i++; r_i++;
     }
   }
  for (m_i = 0; m_i < local_n; m_i++)</pre>
     my keys[m i] = temp keys[m i];
 /* Merge_low */
```



# **Run-times of parallel odd-even**

#### sort

	Number of Keys (in thousands)				
Processes	200	400	800	1600	3200
1	88	190	390	830	1800
2	43	91	190	410	860
4	22	46	96	200	430
8	12	24	51	110	220
16	7.5	14	29	60	130

(times are in milliseconds)



# **Concluding Remarks (1)**

- MPI or the Message-Passing Interface is a library of functions that can be called from C, C++, or Fortran programs.
- A communicator is a collection of processes that can send messages to each other.
- Many parallel programs use the singleprogram multiple data or SPMD approach.



# **Concluding Remarks (2)**

- Most serial programs are deterministic: if we run the same program with the same input we'll get the same output.
- Parallel programs often don't possess this property.
- Collective communications involve all the processes in a communicator.



# **Concluding Remarks (3)**

- When we time parallel programs, we're usually interested in elapsed time or "wall clock time".
- Speedup is the ratio of the serial run-time to the parallel run-time.
- Efficiency is the speedup divided by the number of parallel processes.



# **Concluding Remarks (4)**

- If it's possible to increase the problem size (n) so that the efficiency doesn't decrease as p is increased, a parallel program is said to be scalable.
- An MPI program is unsafe if its correct behavior depends on the fact that MPI\_Send is buffering its input.

