

## Física Quântica / Interações Atômicas e Moleculares: Integrais Úteis

$$\int \sin^2 x \, dx = \frac{1}{2} \left( x - \frac{\sin 2x}{2} \right) + C = \frac{1}{2} (x - \sin x \cos x) + C$$

$$\int \cos^2 x \, dx = \frac{1}{2} \left( x + \frac{\sin 2x}{2} \right) + C = \frac{1}{2} (x + \sin x \cos x) + C$$

$$\int \sin x \cos x \, dx = -\frac{1}{4} \cos 2x + C$$

$$\int_0^{\infty} x^n e^{-x} \, dx = n!$$

$$\int_{-\infty}^{\infty} e^{-x^2} \, dx = \frac{1}{2} \sqrt{\pi}$$

$$\int_{-\infty}^{\infty} x^2 e^{-x^2} \, dx = \frac{1}{4} \sqrt{\pi}$$

$$\text{geral: } \int_{-\infty}^{\infty} x^n e^{-x^2} \, dx = \begin{cases} \frac{n!}{(n/2)! 2^{n+1}} \sqrt{\pi} & \text{para } n \text{ par} \\ 0 & \text{para } n \text{ impar} \end{cases}$$